

# Modeling Hadronic Interactions in PYTHIA

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(From October: Monash University, Melbourne)





# What's the aim?



Theory



Experiment

Adjust this to agree with this

- Many interesting **dynamical phenomena** under active investigation (e.g., higher-order quantum corrections, hadronization, electroweak physics, diffraction, hadron structure, ...)
- Strong indications from both theory and experiment, that the mathematical structure of the **Standard Model is incomplete**
- **New physics, where art thou?** (So far, physics at LHC looks  $\sim$  SM)
- We are now going into an era of **high statistics and high precision**

# Event Structure at Colliders

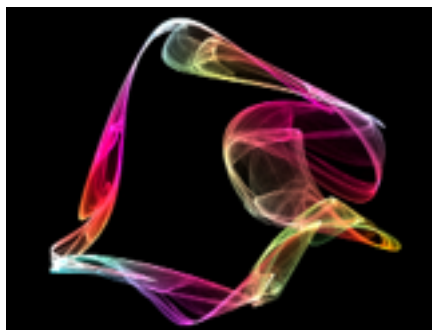
## Dominated by QCD

More than just a perturbative expansion in  $\alpha_s$

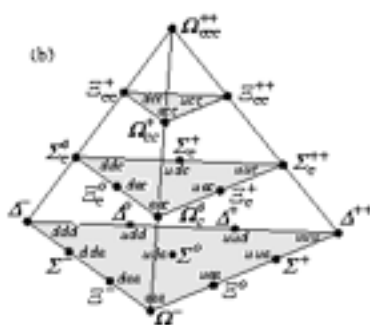
## Emergent phenomena:



**Jets** (the QCD fractal)  $\longleftrightarrow$  amplitude structures  $\longleftrightarrow$  fundamental quantum field theory. Precision jet (structure) studies, jet vetoes.



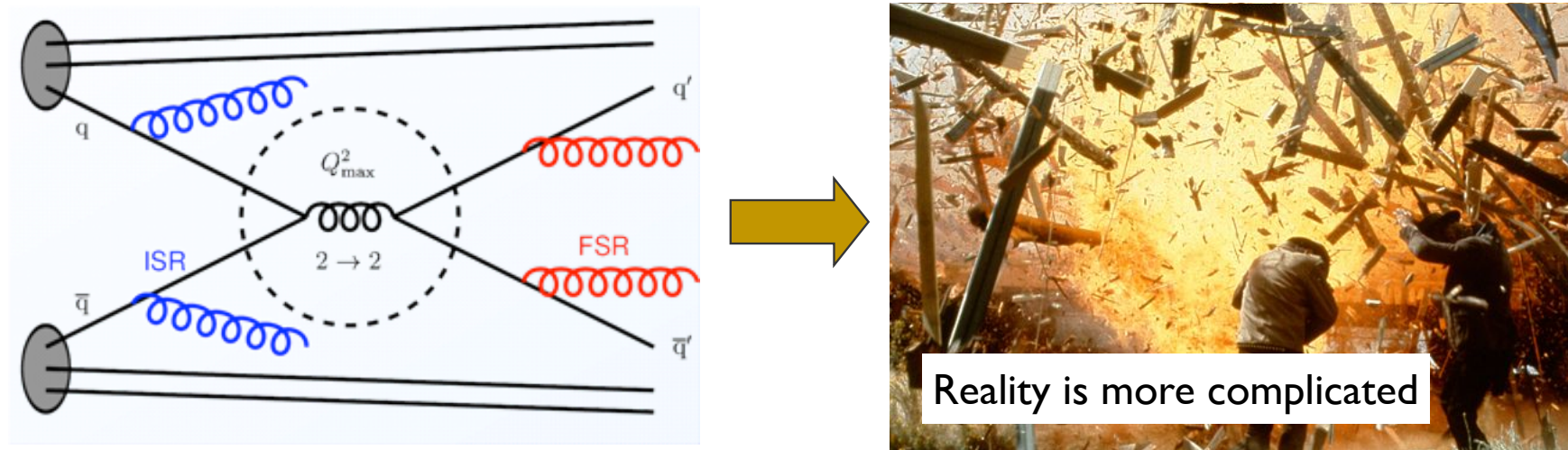
**Strings** (strong gluon fields)  $\longleftrightarrow$  quantum-classical correspondence. String physics. Dynamics of hadronization phase transition. Colour correlations.



**Hadrons**  $\longleftrightarrow$  Spectroscopy (incl excited and exotic states), lattice QCD, (rare) decays, mixing. Identified particles: rates, spectra (FFs), correlations. Hadron beams  $\rightarrow$  PDFs, MPI, diffraction, ...

See eg TASI lectures, e-Print: [arXiv:1207.2389](https://arxiv.org/abs/1207.2389)

# General-Purpose Event Generators



Calculate Everything  $\approx$  solve QCD  $\rightarrow$  requires compromise!

Improve lowest-order perturbation theory,  
by including the 'most significant' corrections  
 $\rightarrow$  complete events (can evaluate any observable you want)

## The Workhorses

PYTHIA : Successor to JETSET (begun in 1978). Originated in hadronization studies: Lund String.  
HERWIG : Successor to EARWIG (begun in 1984). Originated in coherence studies: angular ordering.  
SHERPA : Begun in 2000. Originated in "matching" of matrix elements to showers: CKKW-L.  
+ MORE SPECIALIZED: ALPGEN, MADGRAPH, HELAC, ARIADNE, VINCIA, WHIZARD, (a)MC@NLO, POWHEG, HEJ, PHOJET, EPOS, QGSJET, SIBYLL, DPMJET, LDCMC, DIPSY, HIJING, CASCADE, BLACKHAT, GOSAM, NJETS, ...





# PYTHIA

## PYTHIA anno 1978 (then called JETSET)

LU TP 78-18  
November, 1978

A Monte Carlo Program for Quark Jet  
Generation

T. Sjöstrand, B. Söderberg

A Monte Carlo computer program is  
presented, that simulates the  
fragmentation of a fast parton into a  
jet of mesons. It uses an iterative  
scaling scheme and is compatible with  
the jet model of Field and Feynman.

### **Note:**

Field-Feynman was an early fragmentation model  
Now superseded by the String (in PYTHIA) and  
Cluster (in HERWIG & SHERPA) models.



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```
SUBROUTINE JETGEN(N)
COMMON /JET/ K(100,2), P(100,5)
COMMON /PAR/ PUD, PS1, SIGMA, CX2, EBEG, WFIN, IFLBEG
COMMON /DATA1/ MESO(9,2), CMIX(6,2), PMAS(19)
IFLSGN=(10-IFLBEG)/5
W=2.*EBEG
I=0
IPD=0
C 1 FLAVOUR AND PT FOR FIRST QUARK
IFL1=IABS(IFLBEG)
PT1=SIGMA*SQRT(-ALOG(RANF(0)))
PHI1=6.2832*RANF(0)
PX1=PT1*COS(PHI1)
PY1=PT1*SIN(PHI1)
100 I=I+1
C 2 FLAVOUR AND PT FOR NEXT ANTIQUARK
IFL2=1+INT(RANF(0)/PUD)
PT2=SIGMA*SQRT(-ALOG(RANF(0)))
PHI2=6.2832*RANF(0)
PX2=PT2*COS(PHI2)
PY2=PT2*SIN(PHI2)
C 3 MESON FORMED, SPIN ADDED AND FLAVOUR MIXED
K(I,1)=MESO(3*(IFL1-1)+IFL2,IFLSGN)
ISPIN=INT(PS1+RANF(0))
K(I,2)=1+9*ISPIN+K(I,1)
IF(K(I,1).LE.6) GOTO 110
TMIX=RANF(0)
KM=K(I,1)-6+3*ISPIN
K(I,2)=8+9*ISPIN+INT(TMIX+CMIX(KM,1))+INT(TMIX+CMIX(KM,2))
C 4 MESON MASS FROM TABLE, PT FROM CONSTITUENTS
110 P(I,5)=PMAS(K(I,2))
P(I,1)=PX1+PX2
P(I,2)=PY1+PY2
PMTS=P(I,1)**2+P(I,2)**2+P(I,5)**2
C 5 RANDOM CHOICE OF X=(E+PZ)MESON/(E+PZ)AVAILABLE GIVES E AND PZ
X=RANF(0)
IF(RANF(0).LT.CX2) X=1.-X**(1./3.)
P(I,3)=(X*W-PMTS/(X*W))/2.
P(I,4)=(X*W+PMTS/(X*W))/2.
C 6 IF UNSTABLE, DECAY CHAIN INTO STABLE PARTICLES
120 IPD=IPD+1
IF(K(IPD,2).GE.8) CALL DECAY(IPD,I)
IF(IPD.LT.1.AND.I.LE.96) GOTO 120
C 7 FLAVOUR AND PT OF QUARK FORMED IN PAIR WITH ANTIQUARK ABOVE
IFL1=IFL2
PX1=-PX2
PY1=-PY2
C 8 IF ENOUGH E+PZ LEFT, GO TO 2
W=(1.-X)*W
IF(W.GT.WFIN.AND.I.LE.95) GOTO 100
N=I
RETURN
END
```





# PYTHIA

## PYTHIA anno 2014

(now called PYTHIA 8)

~ 100,000 lines of C++

What a modern MC generator has inside:

LU TP 07-28 (CPC 178 (2008) 852)  
October, 2007

A Brief Introduction to PYTHIA 8.1

T. Sjöstrand, S. Mrenna, P. Skands

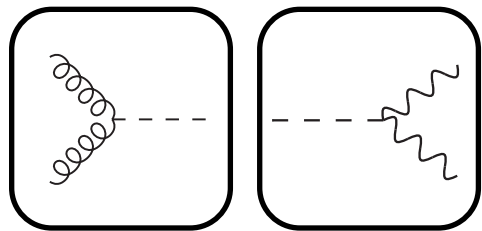
The Pythia program is a standard tool for the generation of high-energy collisions, comprising a coherent set of physics models for the evolution from a few-body hard process to a complex multihadronic final state. It contains a library of hard processes and models for initial- and final-state parton showers, multiple parton-parton interactions, beam remnants, string fragmentation and particle decays. It also has a set of utilities and interfaces to external programs. [...]

- Hard Processes (internal, interfaced, or via Les Houches events)
- BSM (internal or via interfaces)
- PDFs (internal or via interfaces)
- Showers (internal or inherited)
- Multiple parton interactions
- Beam Remnants
- String Fragmentation
- Decays (internal or via interfaces)
- Examples and Tutorial
- Online HTML / PHP Manual
- Utilities and interfaces to external programs

# Divide and Conquer

**Factorization** → Split the problem into many (nested) pieces  
+ **Quantum mechanics** → Probabilities → Random Numbers (MC)

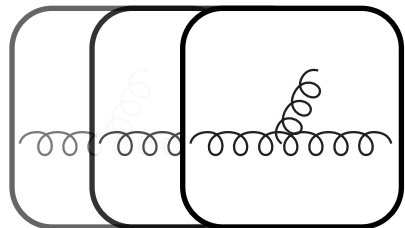
$$\mathcal{P}_{\text{event}} = \mathcal{P}_{\text{hard}} \otimes \mathcal{P}_{\text{dec}} \otimes \mathcal{P}_{\text{ISR}} \otimes \mathcal{P}_{\text{FSR}} \otimes \mathcal{P}_{\text{MPI}} \otimes \mathcal{P}_{\text{Had}} \otimes \dots$$



## Hard Process & Decays:

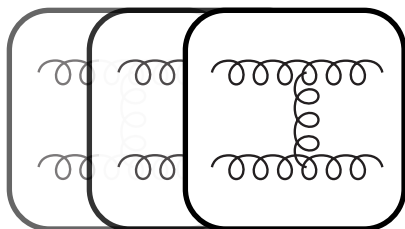
Use (N)LO matrix elements

→ Sets "hard" resolution scale for process:  $Q_{\text{MAX}}$



## Initial- & Final-State Radiation (ISR & FSR):

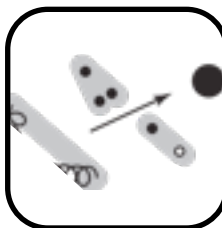
Altarelli-Parisi equations → differential evolution,  $dP/dQ^2$ , as function of resolution scale; run from  $Q_{\text{MAX}}$  to  $\sim 1$  GeV



## MPI (Multi-Parton Interactions)

Additional (soft) parton-parton interactions: LO matrix elements

→ Additional (soft) "Underlying-Event" activity



## Hadronization

Non-perturbative model of color-singlet parton systems → hadrons

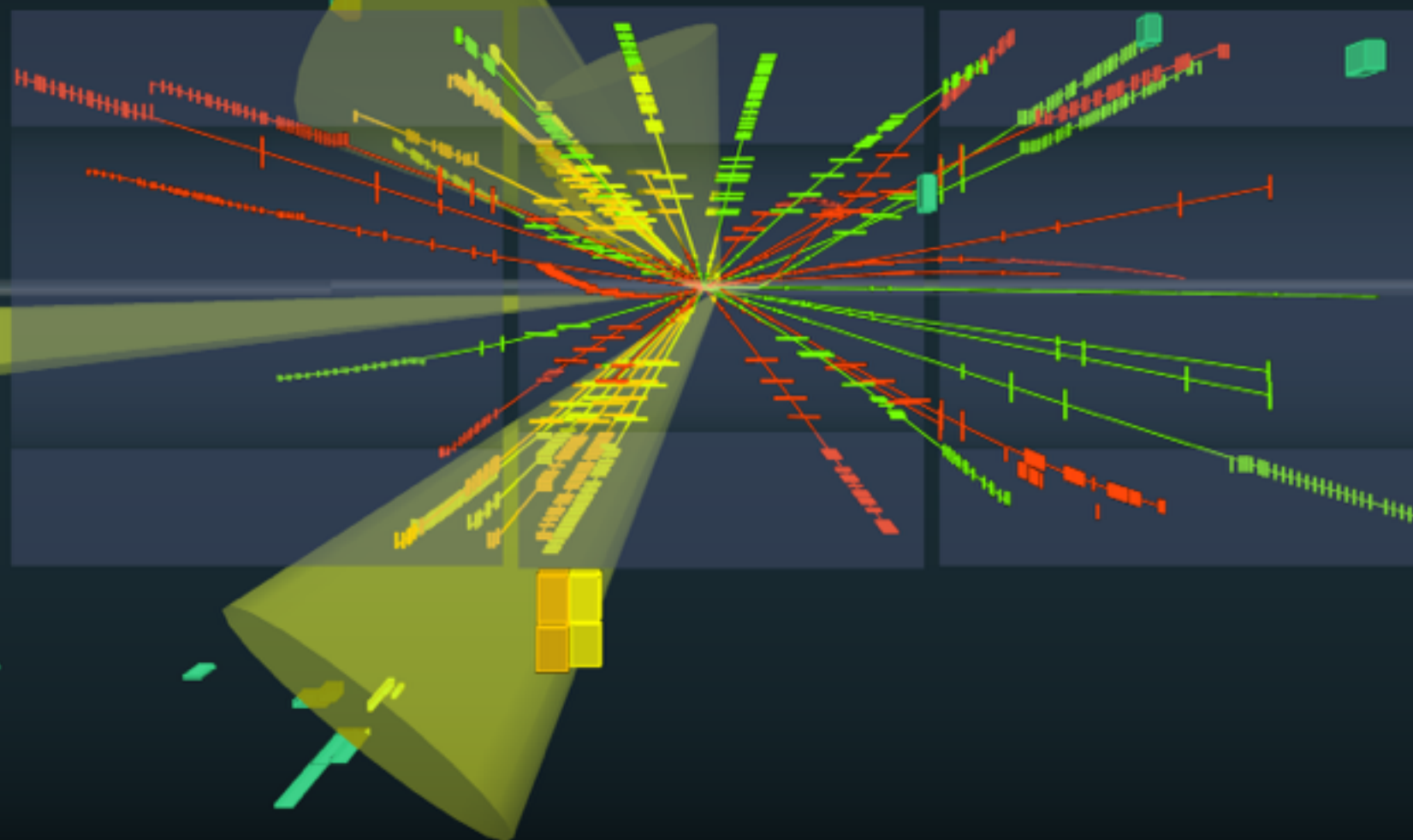


# Bremsstrahlung

a.k.a. Initial- and Final-state radiation

a.k.a. Parton Showers

cf. equivalent-photon  
approximation  
Weizsäcker, Williams  
~ 1934

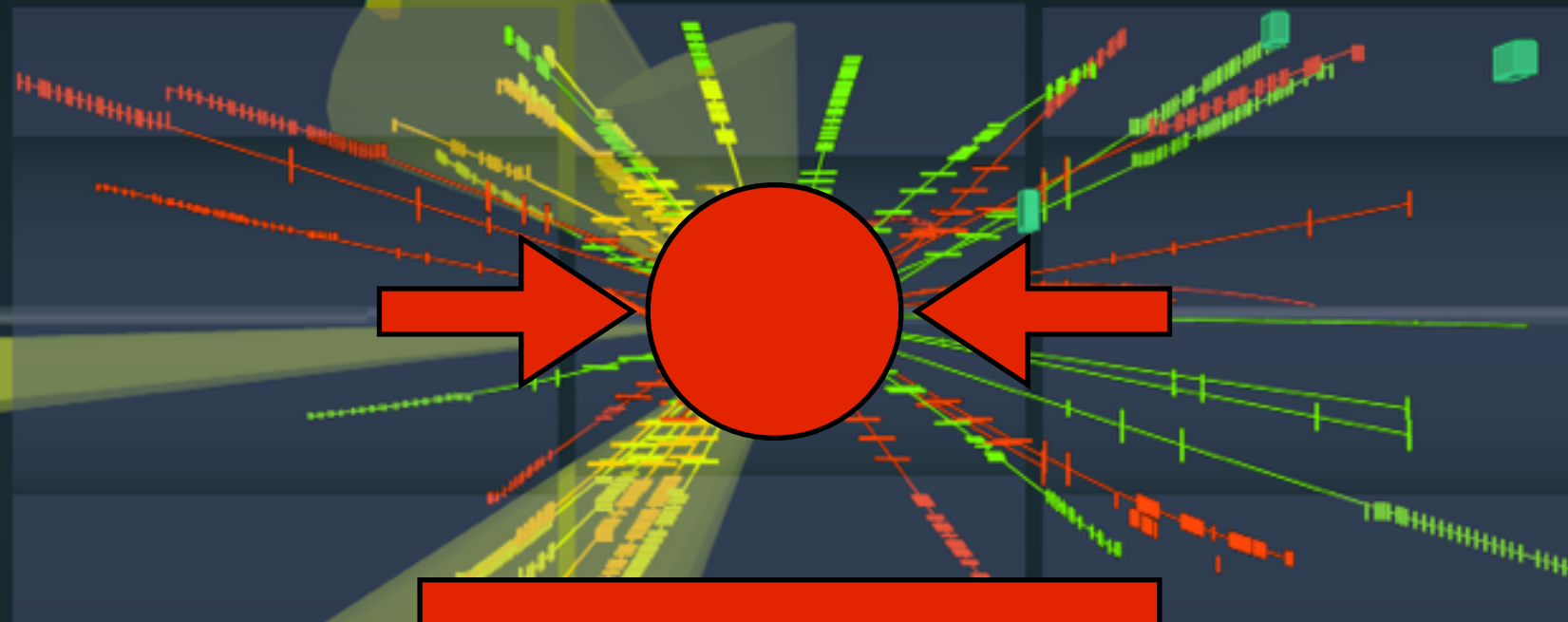


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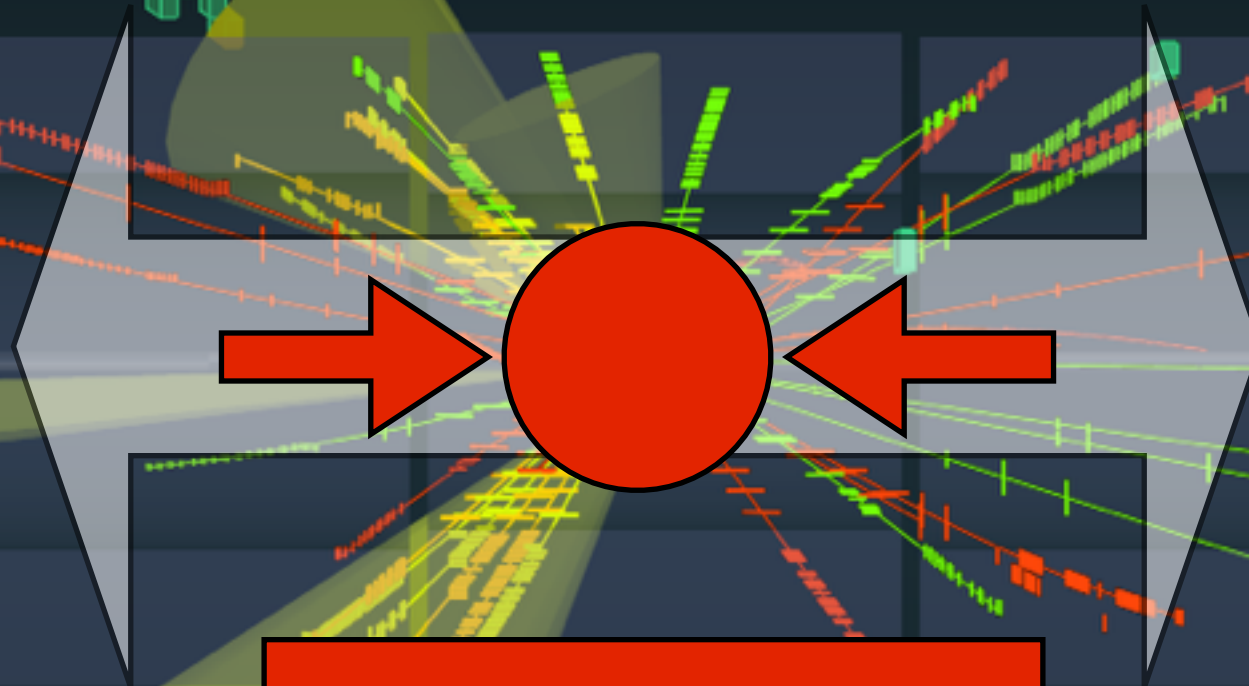
Accelerated  
Charges



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Accelerated  
Charges

Associated field  
(fluctuations) continues

Collision Energy

482137

nl

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Radiation

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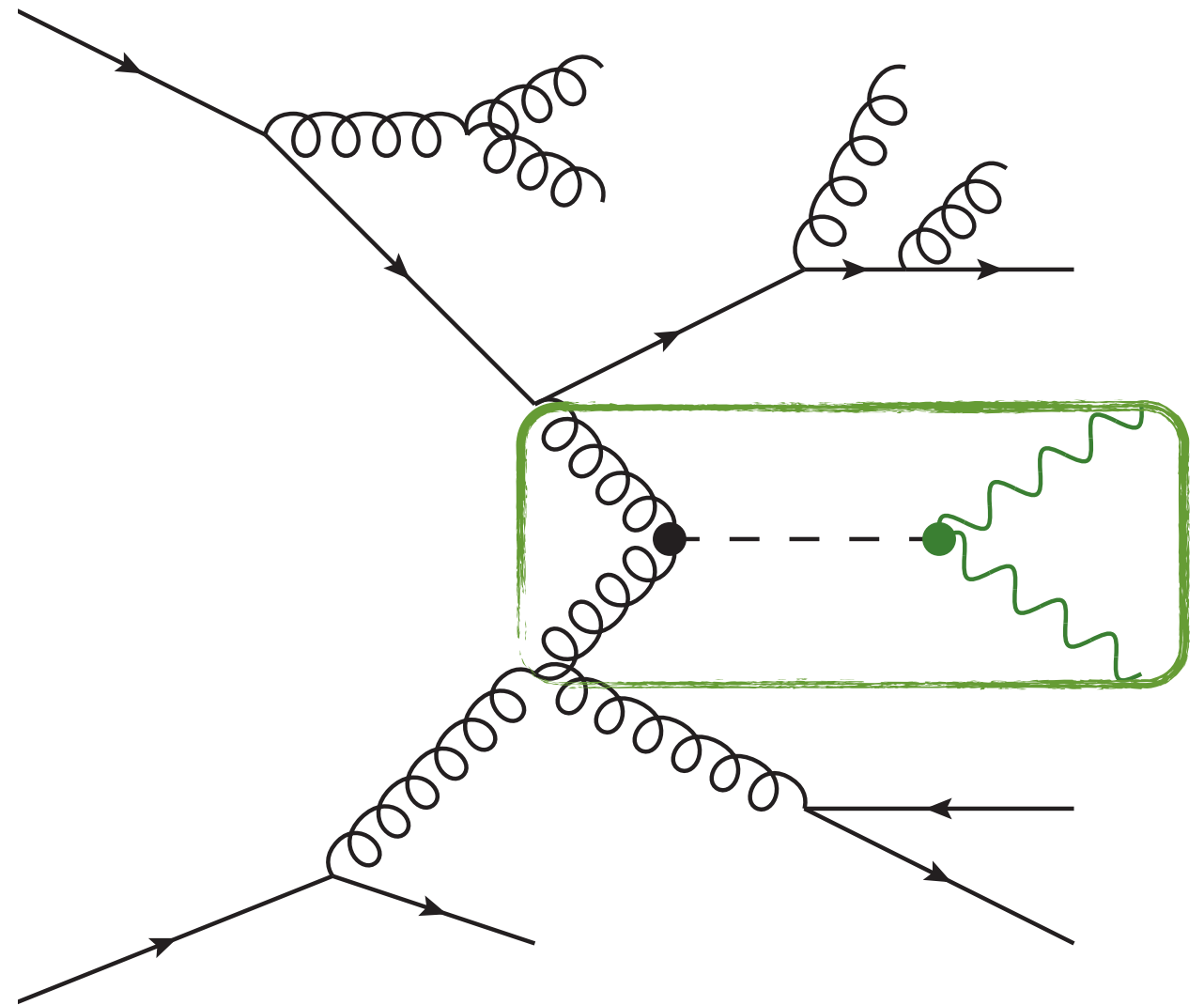
Accelerated  
Charges

The harder they get kicked, the harder the  
fluctuations that continue to become strahlung

# Jets $\approx$ Fractals

**Most bremsstrahlung** is driven by divergent propagators  $\rightarrow$  simple structure

**Amplitudes factorize in singular limits** ( $\rightarrow$  universal “conformal” or “fractal” structure)

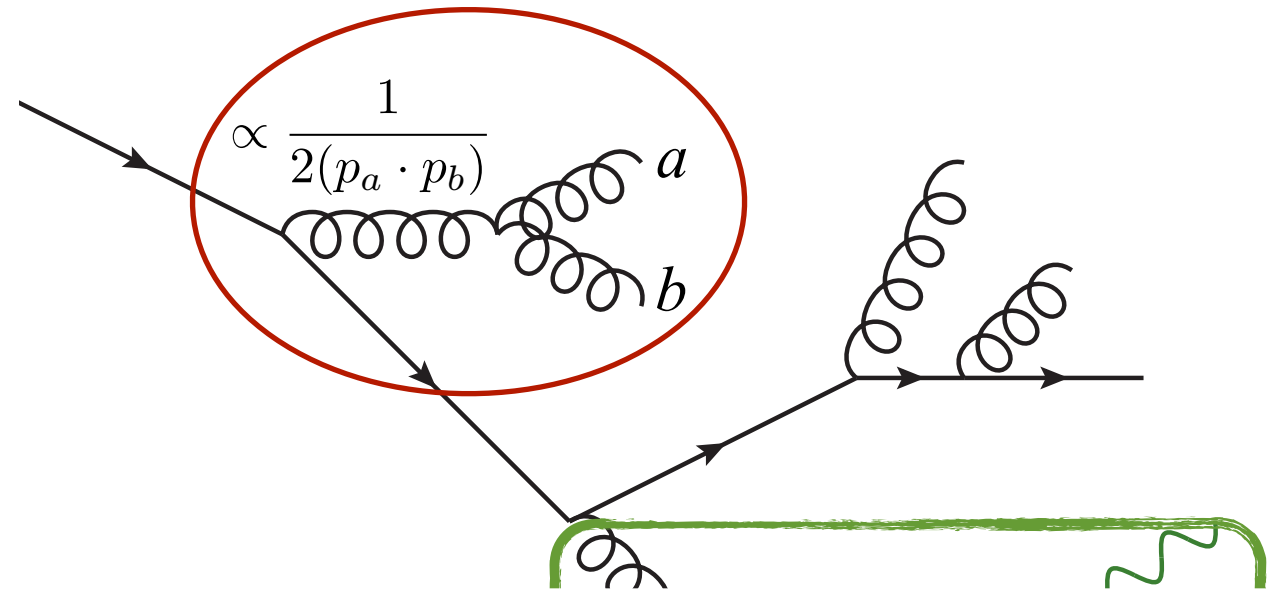


See: PS, *Introduction to QCD*, TASI 2012, [arXiv:1207.2389](https://arxiv.org/abs/1207.2389)

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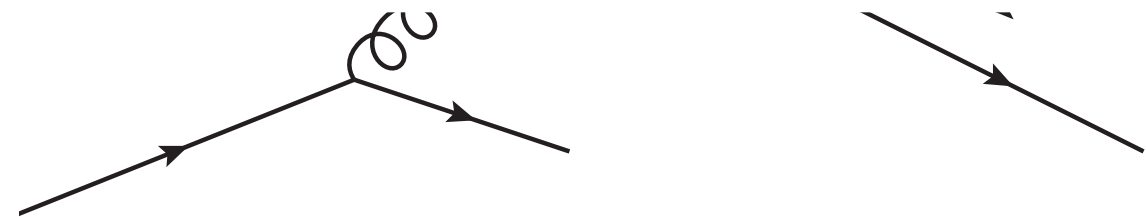
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Partons  $ab \rightarrow$   
"collinear":

$P(z) =$  DGLAP splitting kernels, with  $z =$  energy fraction  $= E_a/(E_a+E_b)$

$$|\mathcal{M}_{F+1}(\dots, a, b, \dots)|^2 \xrightarrow{a||b} g_s^2 C \frac{P(z)}{2(p_a \cdot p_b)} |\mathcal{M}_F(\dots, a+b, \dots)|^2$$



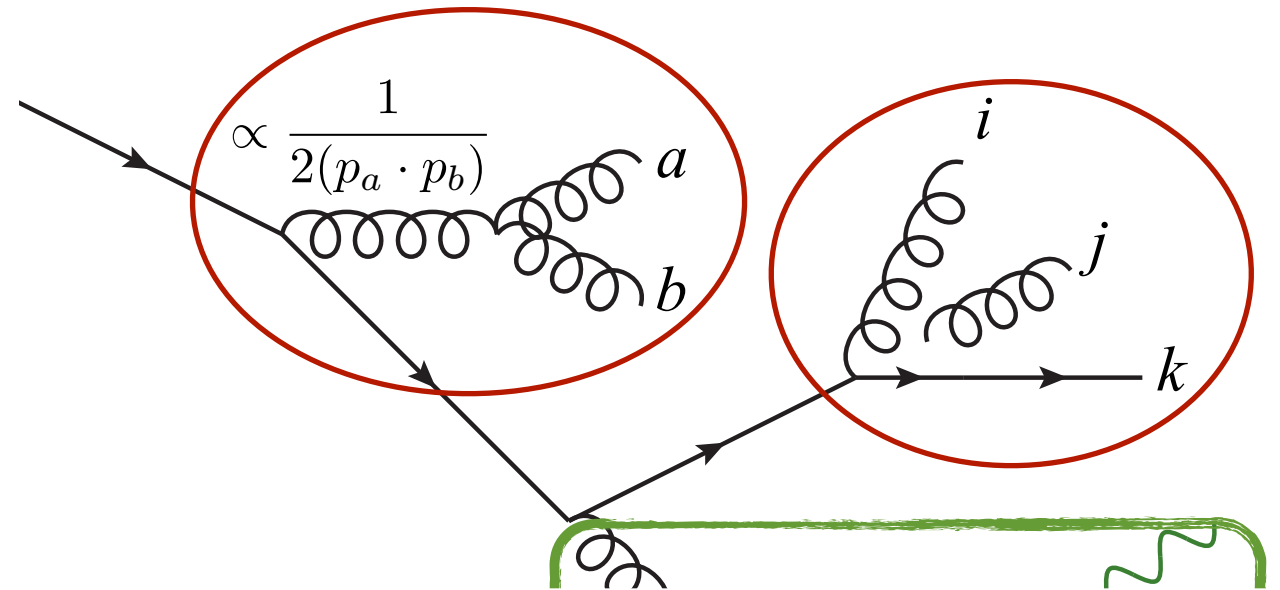
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Gluon  $j \rightarrow$  “soft”:

Coherence  $\rightarrow$  Parton  $j$  really emitted by  $(i,k)$  “colour antenna”

$$|\mathcal{M}_{F+1}(\dots, i, j, k, \dots)|^2 \xrightarrow{j_g \rightarrow 0} g_s^2 C \frac{(p_i \cdot p_k)}{(p_i \cdot p_j)(p_j \cdot p_k)} |\mathcal{M}_F(\dots, i, k, \dots)|^2$$

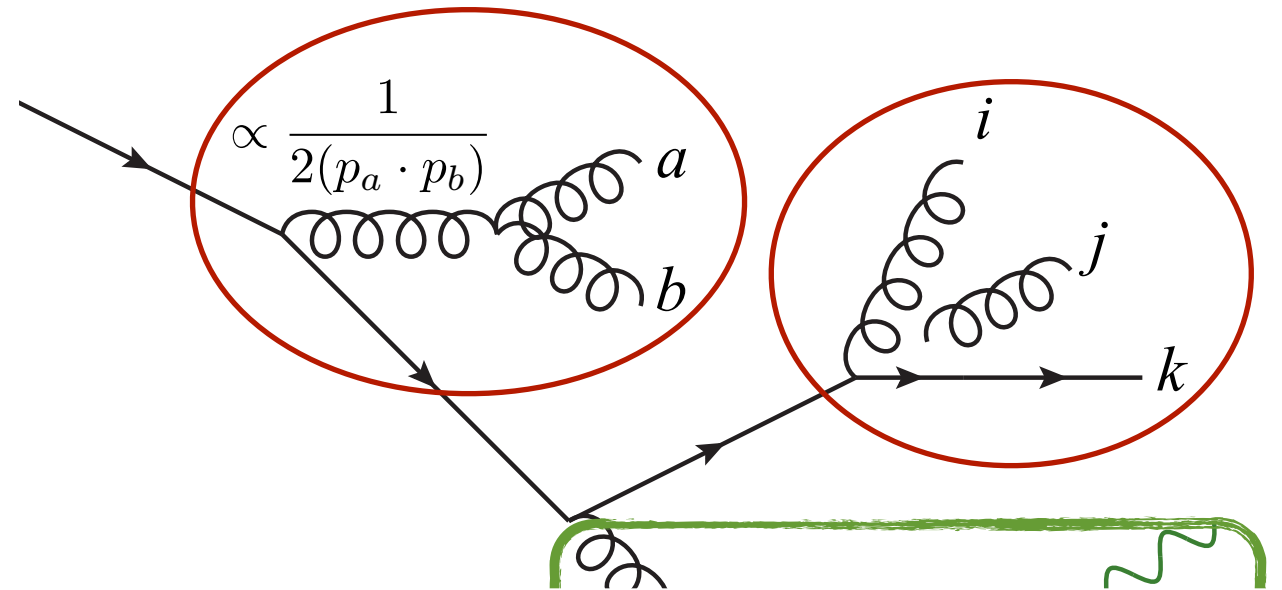
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Can apply this many times  
 $\rightarrow$  nested factorizations

# Factorization

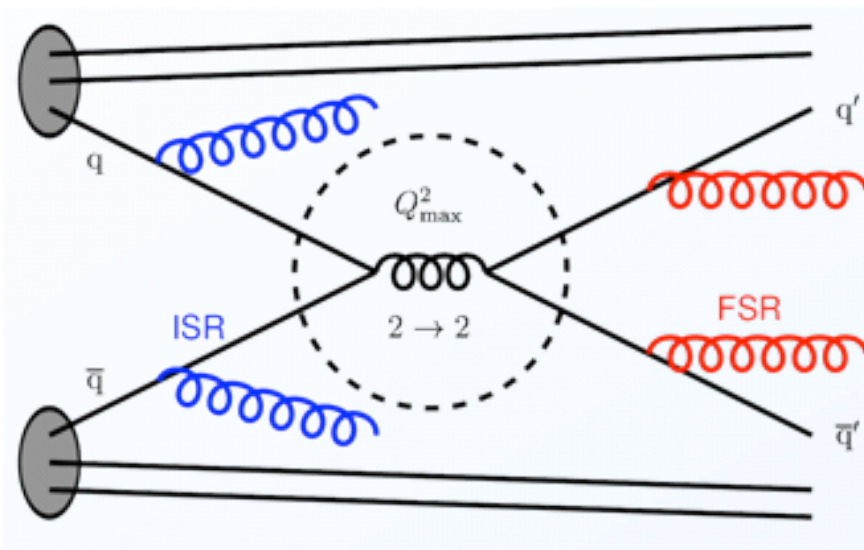
## Factorization of Production and Decay:



Valid up to corrections  $\Gamma/m \rightarrow$  breaks down for large  $\Gamma$

More subtle when colour/charge flows *through* the diagram

## Factorization of Long and Short Distances



Scale of fluctuations inside a hadron

$$\sim \Lambda_{\text{QCD}} \sim 200 \text{ MeV}$$

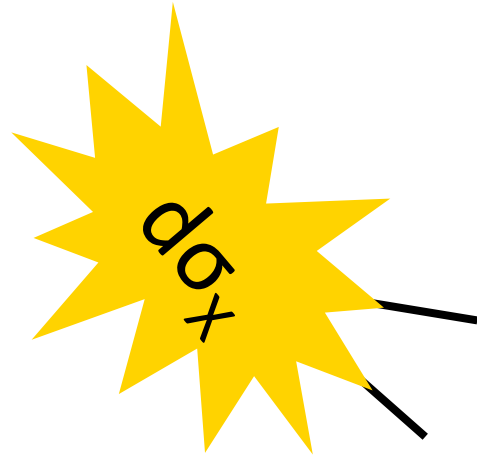
Scale of hard process  $\gg \Lambda_{\text{QCD}}$

$\rightarrow$  proton looks "frozen"

Instantaneous snapshot of long-wavelength structure, independent of nature of hard process

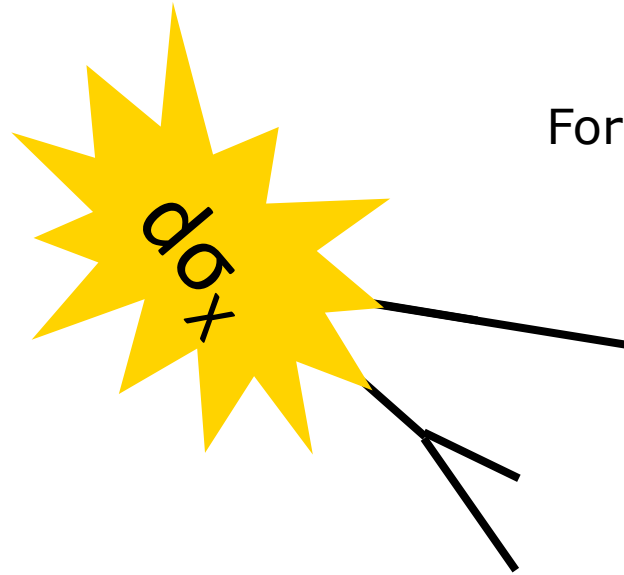


# Practical Examples



For any basic process  $d\sigma_X = \sqrt{\quad}$  (calculated process by process)

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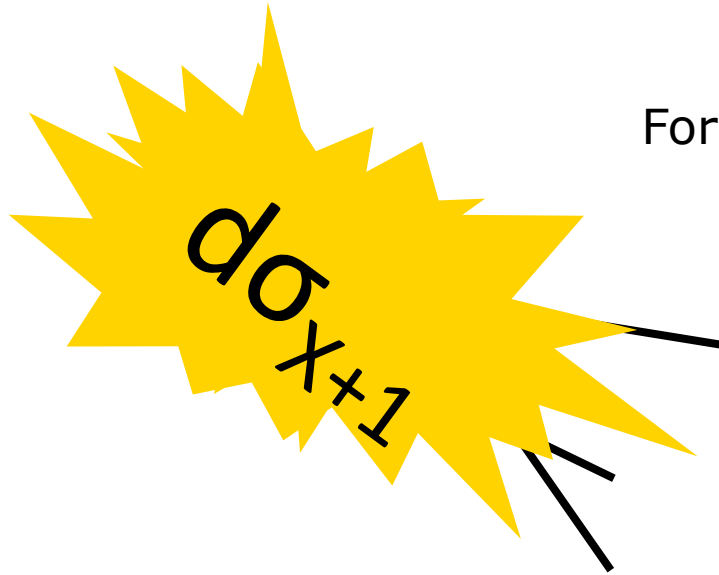
For any basic process  $d\sigma_X = \sqrt{\quad}$  (calculated process by process)

$$d\sigma_{X+1} \sim N_C 2g_s^2 \frac{ds_{i1}}{s_{i1}} \frac{ds_{1j}}{s_{1j}} d\sigma_X$$

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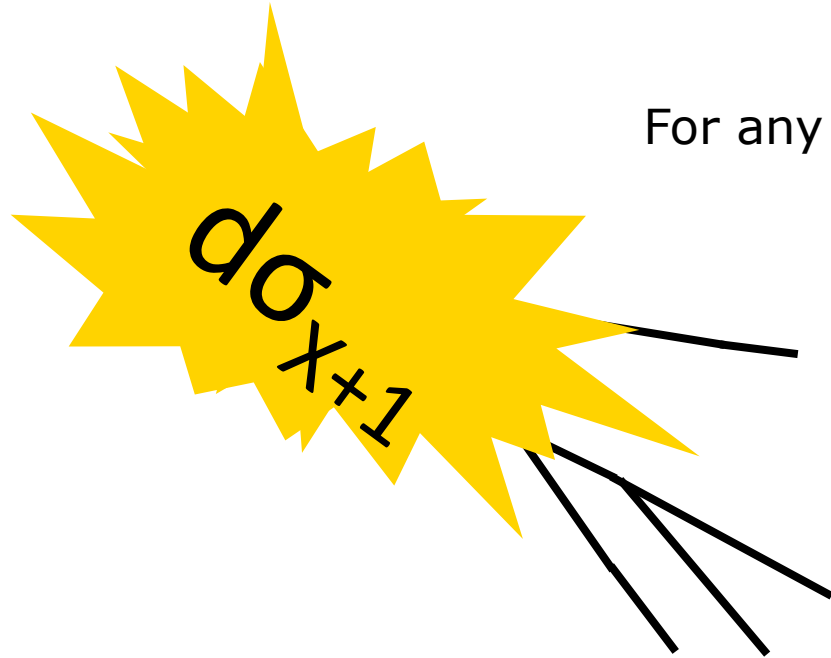
For any basic process  $d\sigma_X = \checkmark$  (calculated process by process)

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**Singularities:** mandated by gauge theory

**Non-singular terms:** process-dependent

$$\frac{|\mathcal{M}(Z^0 \rightarrow q_i g_j \bar{q}_k)|^2}{|\mathcal{M}(Z^0 \rightarrow q_I \bar{q}_K)|^2} = g_s^2 2C_F \left[ \frac{2s_{ik}}{s_{ij}s_{jk}} + \frac{1}{s_{IK}} \left( \frac{s_{ij}}{s_{jk}} + \frac{s_{jk}}{s_{ij}} \right) \right]$$

SOFT                      COLLINEAR

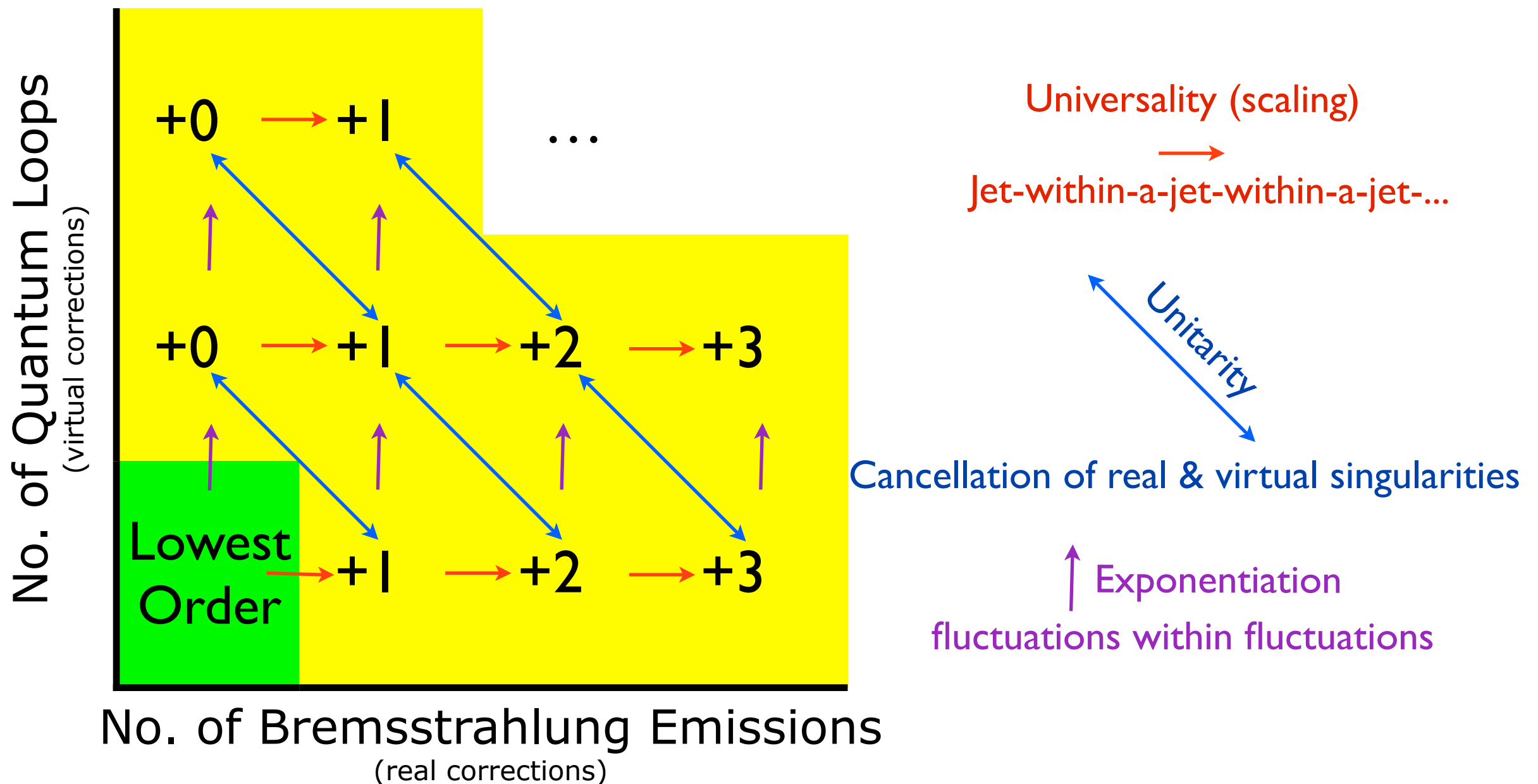
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SOFT                      COLLINEAR+F

# Bootstrapped Perturbation Theory

Start from an **arbitrary lowest-order** process (green = QFT amplitude squared)

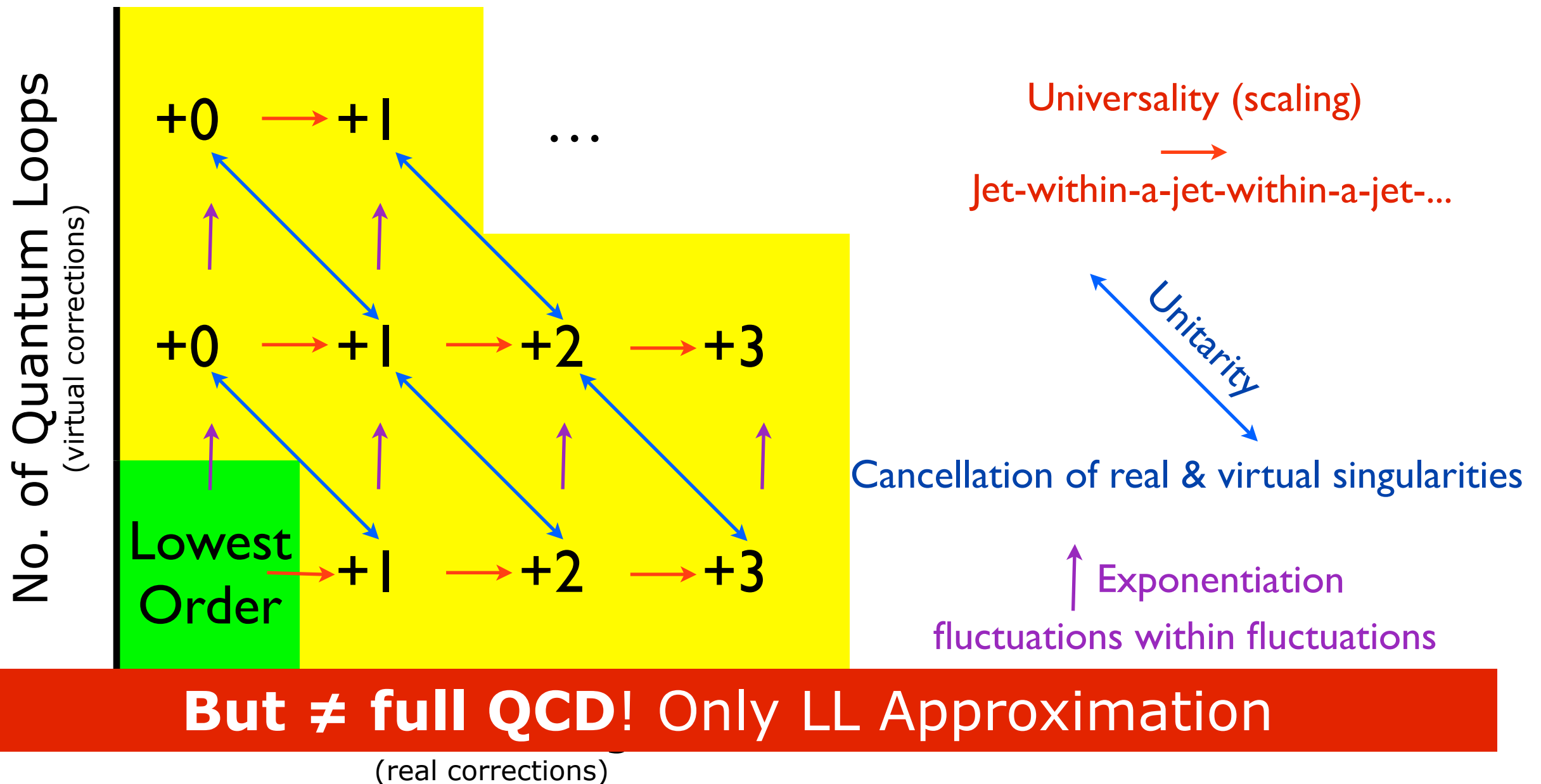
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# Process-Dependence

(Matrix-Element Corrections)



Image Credits: istockphoto



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(Matrix-Element Corrections)

**This talk is not about matrix-element matching.**  
That said, PYTHIA 8 contains a large number of implementations of matching schemes, based on “UserHooks” and Les Houches event files [\[ask S. Prestel\]](#)

Image Credits: istockphoto

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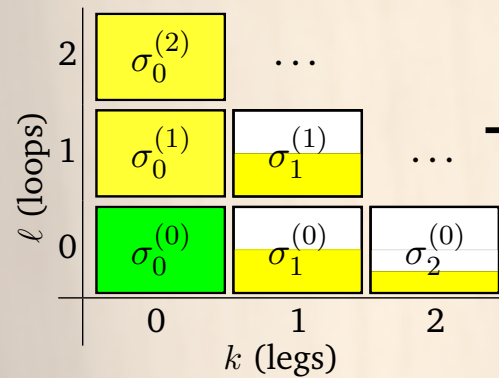


UserHooks gives further possibilities to control event generation / implement new schemes  
Can also implement own processes, decays, or shower model(s) (e.g., VINCIA plug-in)

# Examples

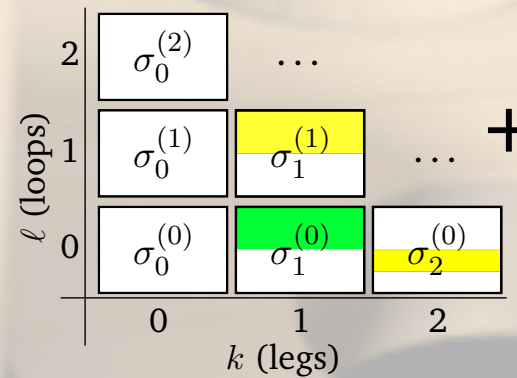
## Slicing: the "MLM" & "CKKW-L" prescriptions

**F @ LO $\times$ LL-Soft (excl)**



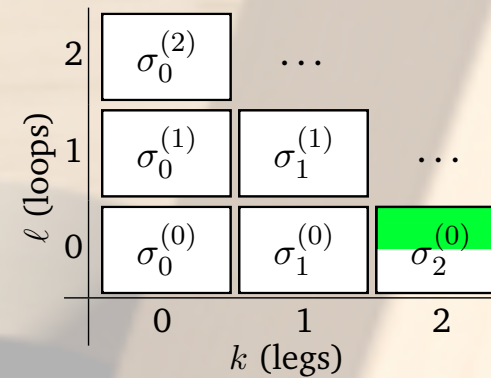
(CKKW & Lönnblad, 2001)

**F+1 @ LO $\times$ LL-Soft (excl)**



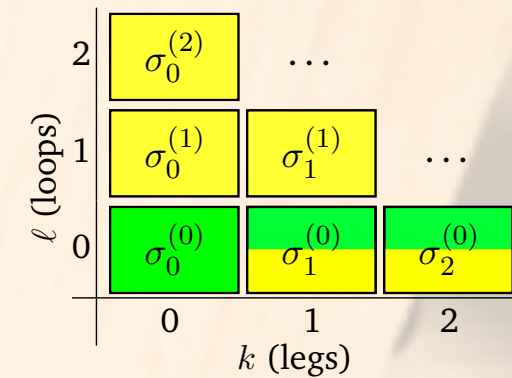
(Mangano, 2002)

**F+2 @ LO $\times$ LL (incl)**



(+many more recent; see Alwall et al., EPJC53(2008)473)

**F @ LO $_2$  $\times$ LL (MLM & (L)-CKKW)**



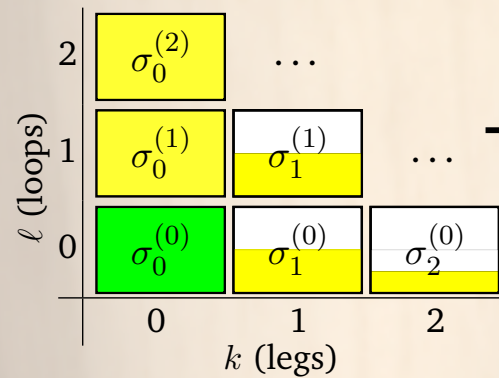
ALPGEN  
HERWIG  
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...



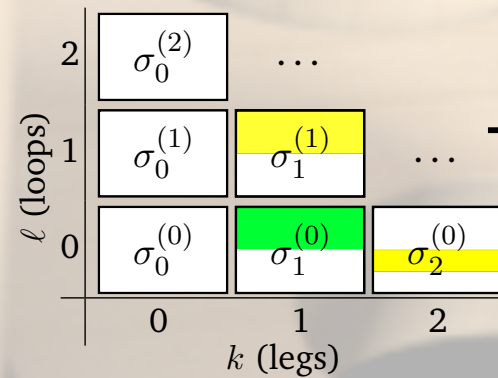
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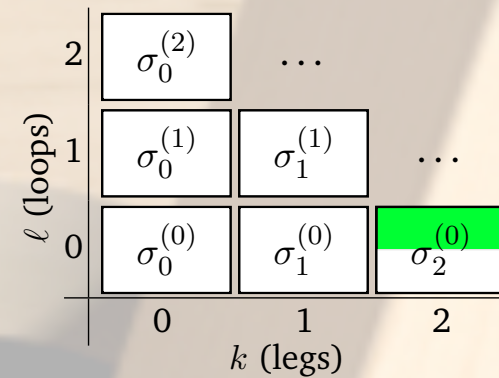
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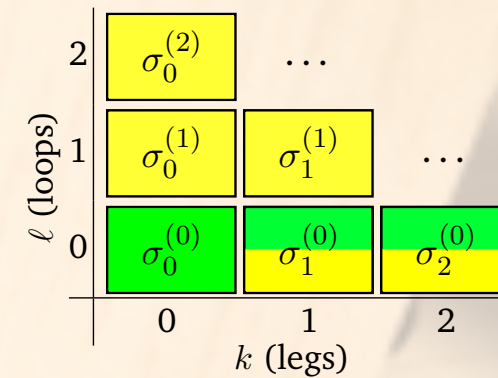
F+1 @ LO×LL-Soft (excl)



F+2 @ LO×LL (incl)



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(CKKW & Lönnblad, 2001)

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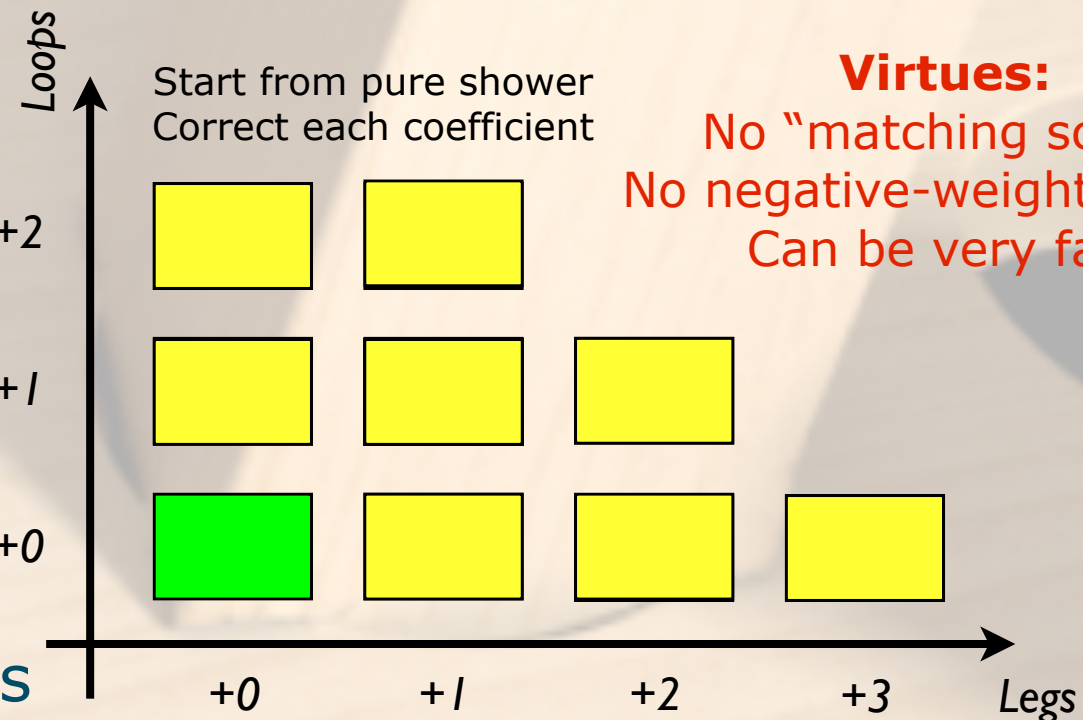
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Reinterpret higher-order matrix elements as radiation functions

Unitarity + Speed

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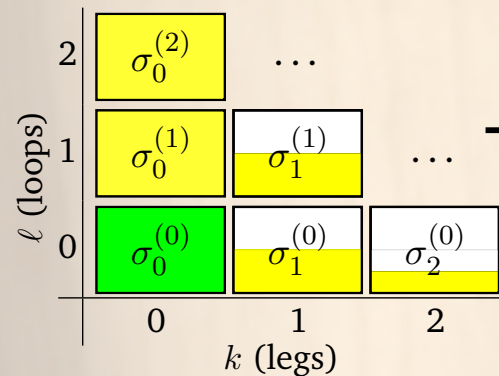
VINCIA

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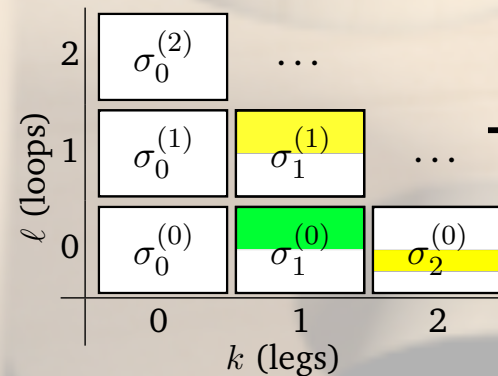
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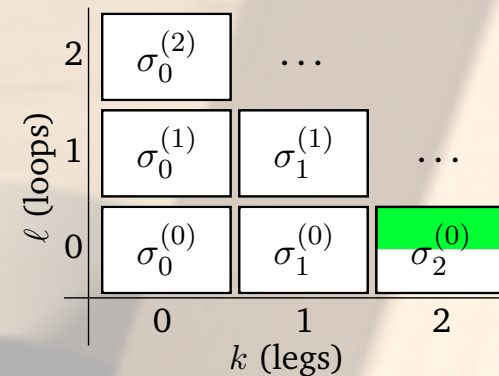
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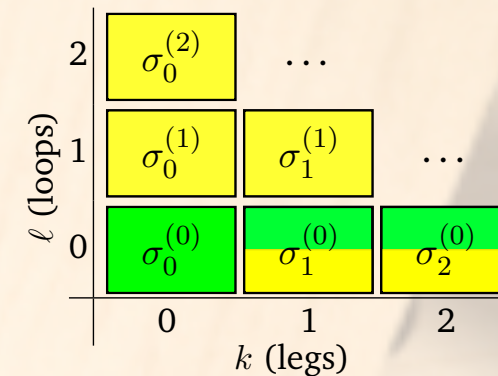
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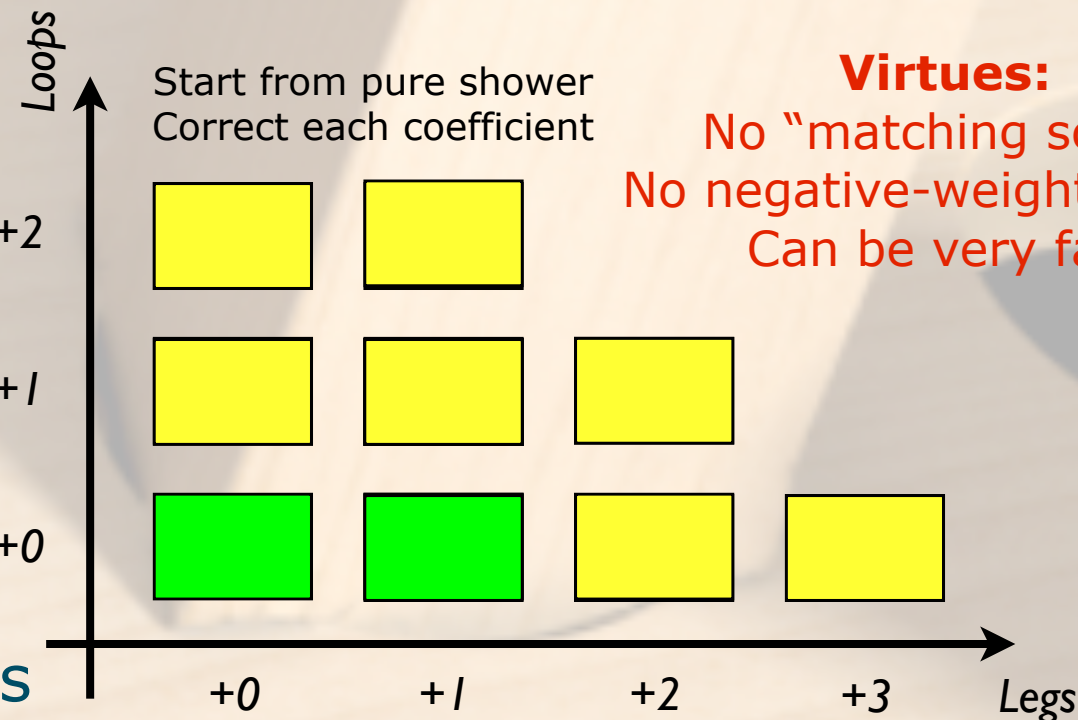
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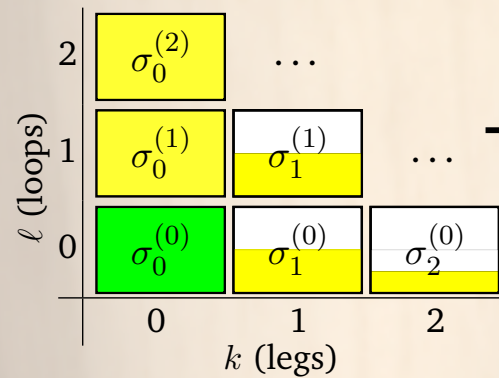
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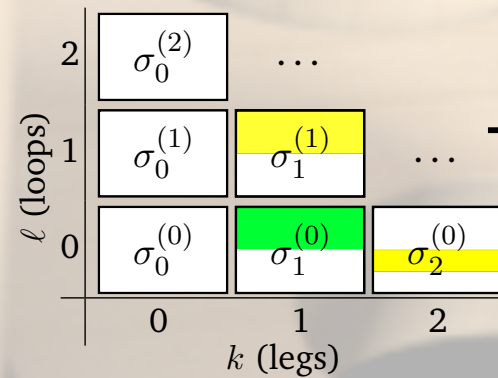
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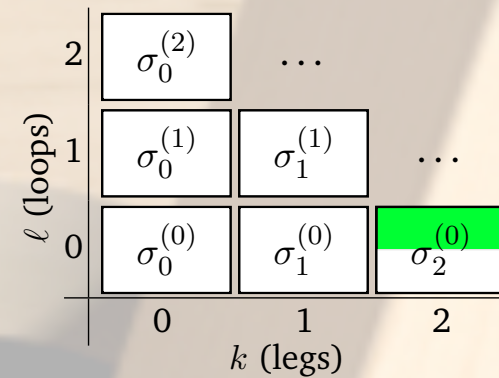
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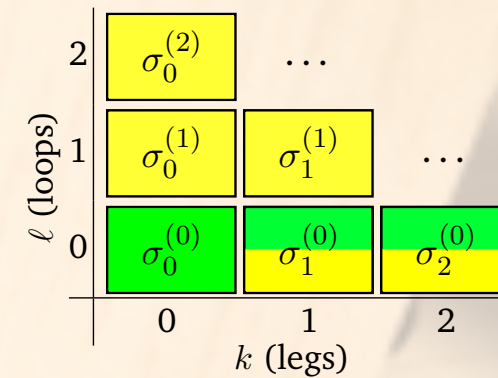
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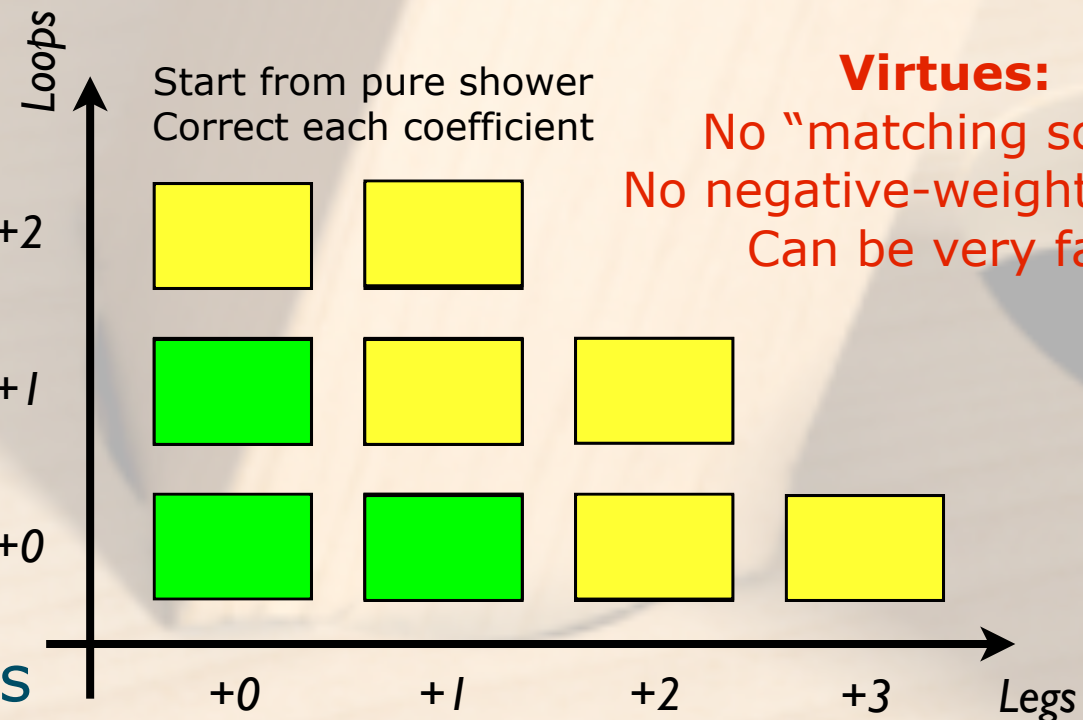
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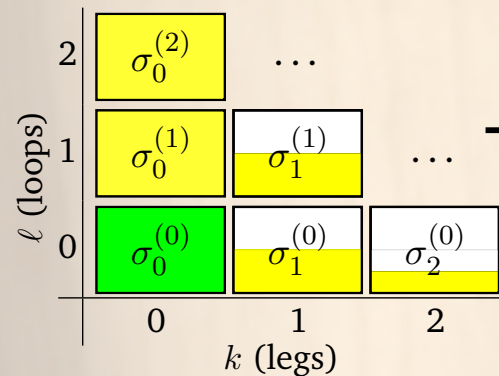
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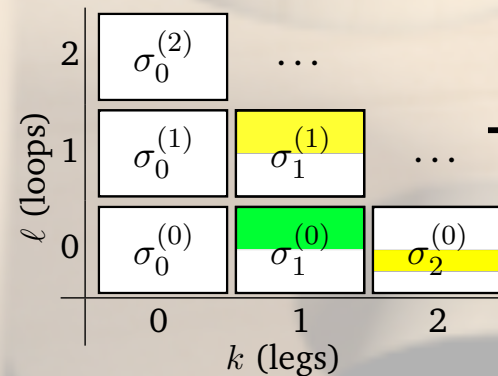
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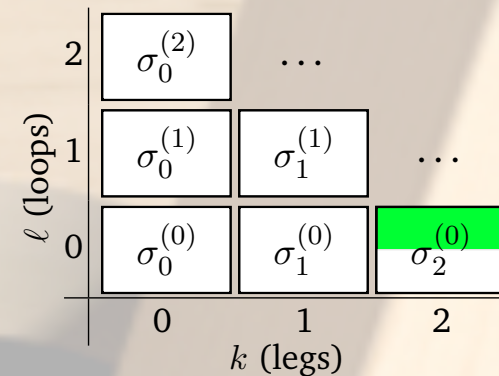
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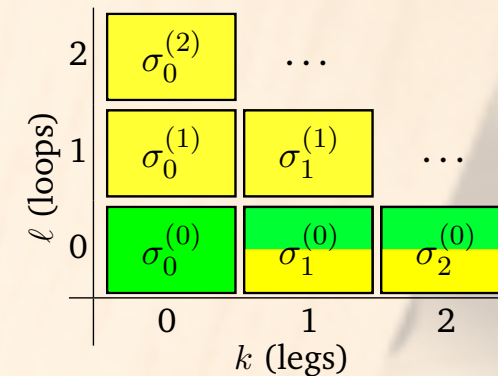
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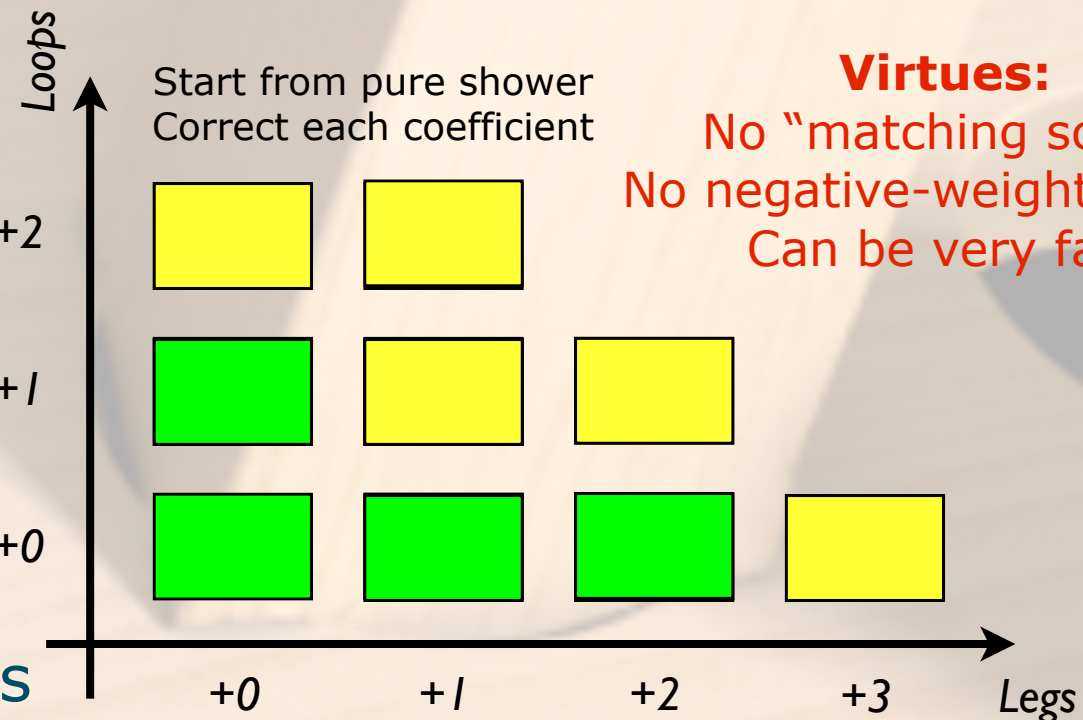
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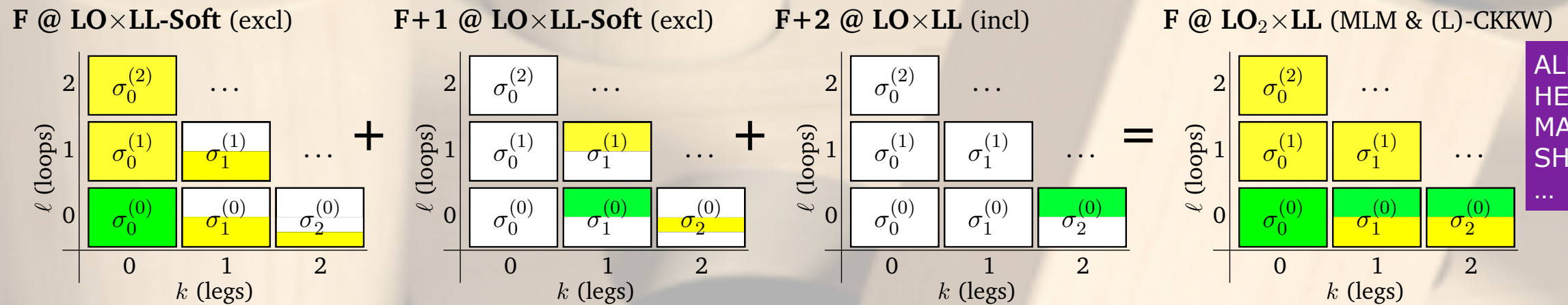
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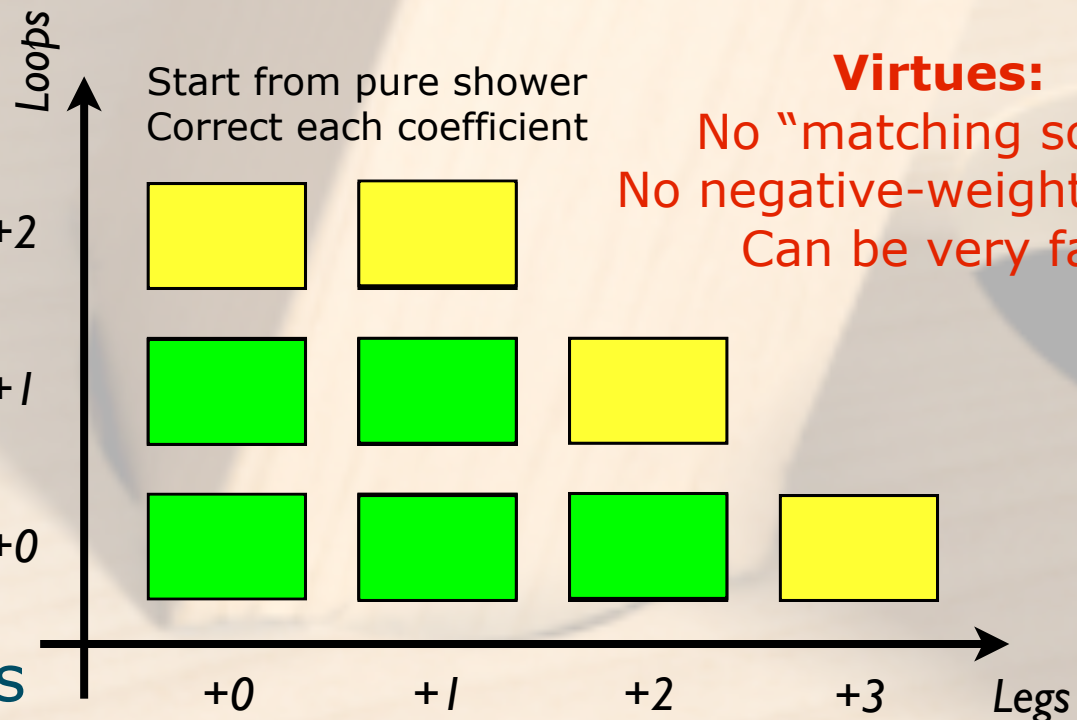
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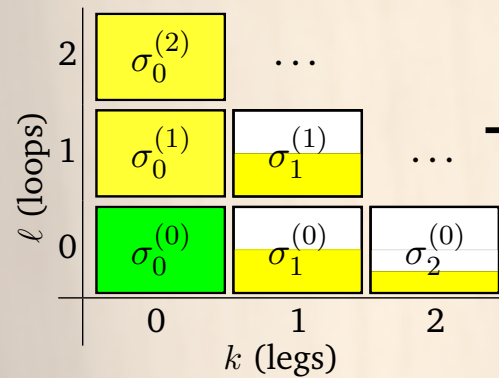
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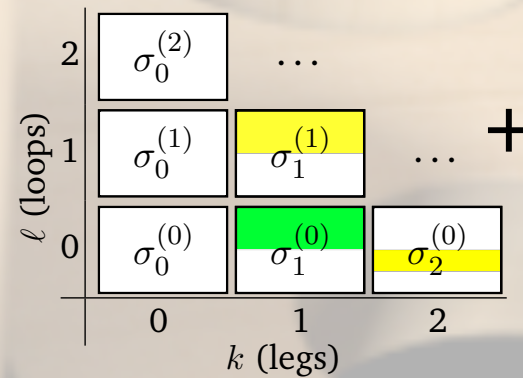
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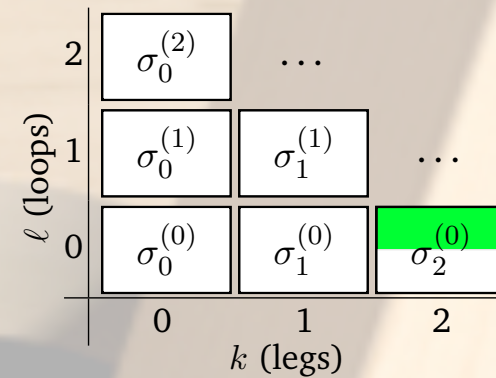
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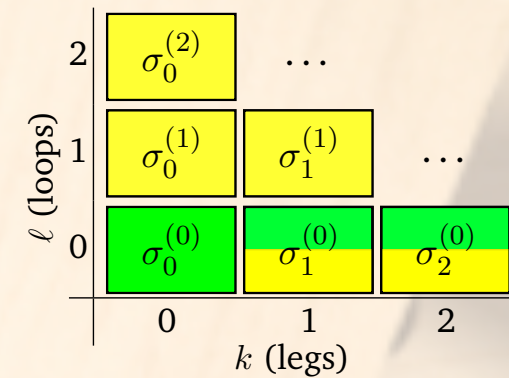
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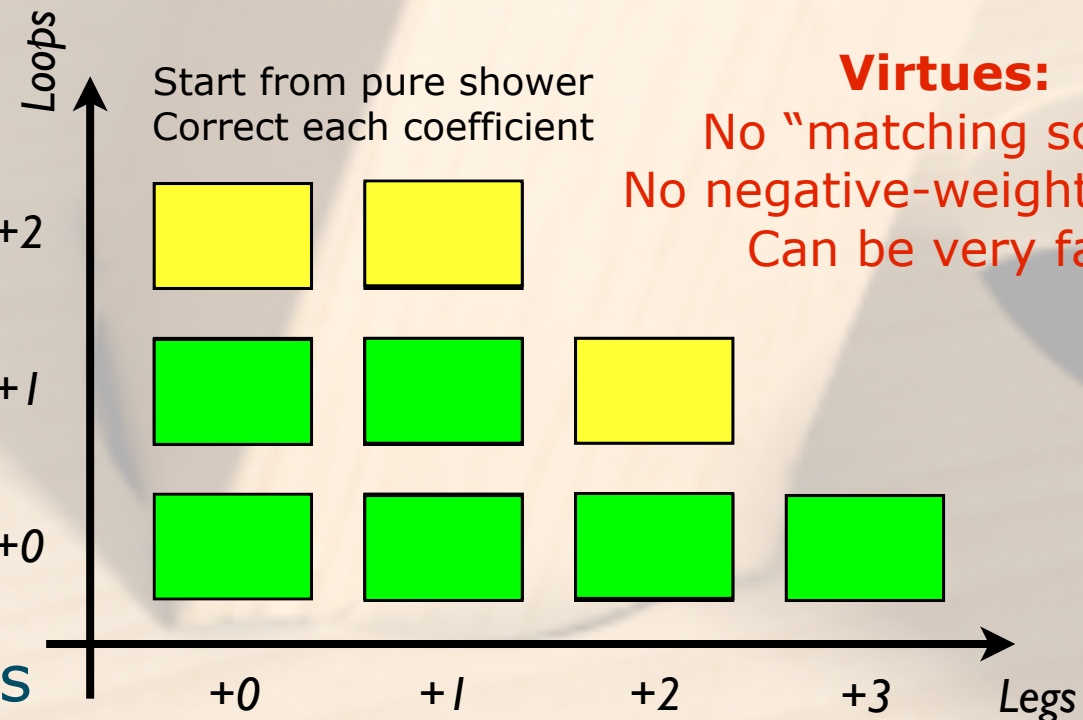
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# Comparison : A Tale of Two Paradigms

**Standard Paradigm:** consider a single physical system; a single physical process

Explicit solutions (to given perturbative order)

Standard-Model: typically NLO or NNLO

Beyond-SM: typically LO or NLO

LO: Leading Order (Born)  
NLO = Next-to-LO, ...

Limited generality

**Shower Paradigm:** consider all possible physical processes (within perturbative QFT)

Approximate solutions

Process-dependence = subleading correction ( $\rightarrow$  matching)

Maximum generality

Emphasis is on universalities; physics

Common property of all processes is, for instance, limits in which they factorize!



# Hadronization





# Hadronization



→ how do coloured partons (quarks and gluons)  
turn into colourless hadrons ...

# From Partons to Pions

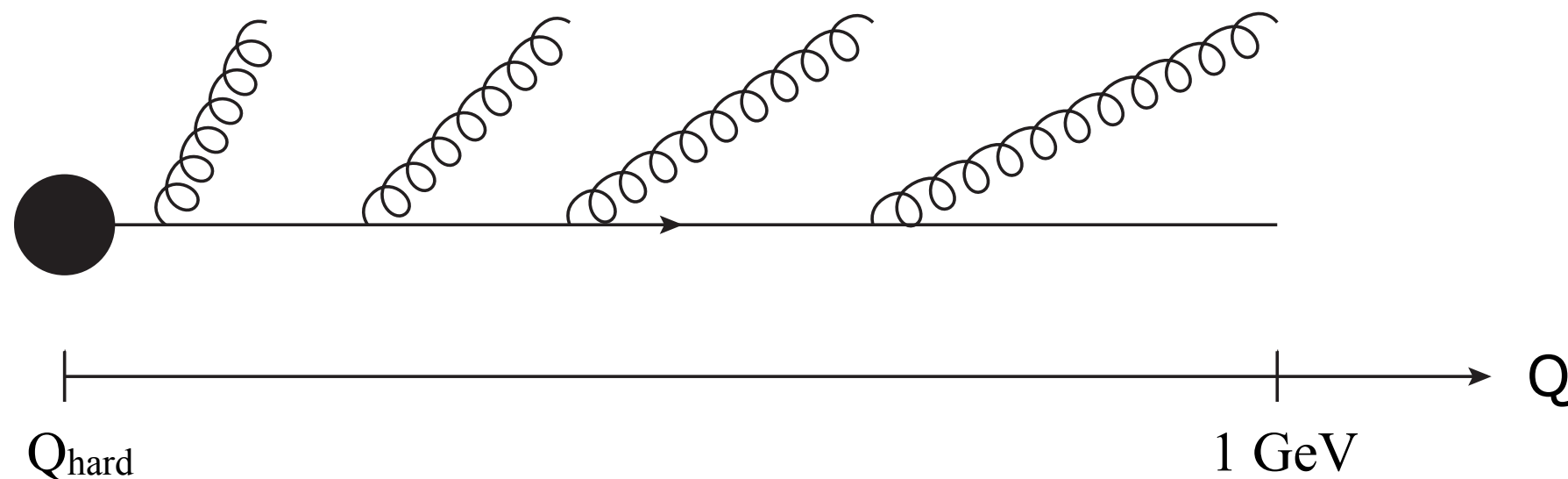
... the fragmentation of a fast parton into a jet ...

**Fast:** It starts at a high factorization scale

$$Q = Q_F = Q_{\text{hard}}$$

It showers  
(perturbative  
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It ends up  
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 $Q \sim m_\rho \sim 1 \text{ GeV}$





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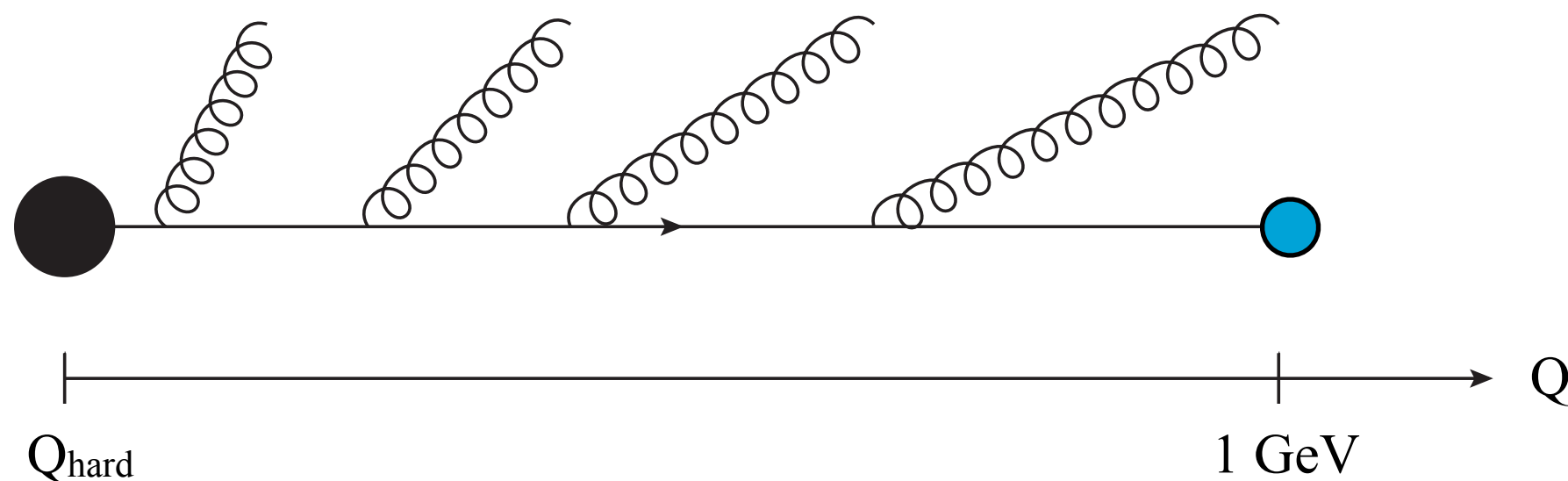
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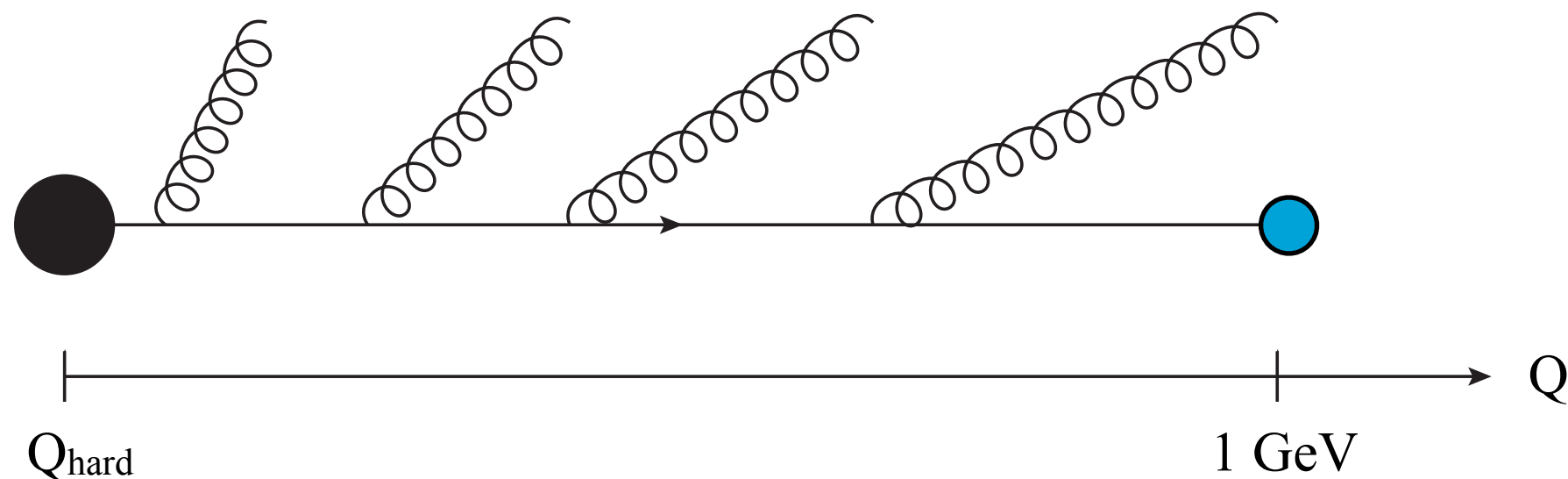
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→ "Local Parton-Hadron Duality"

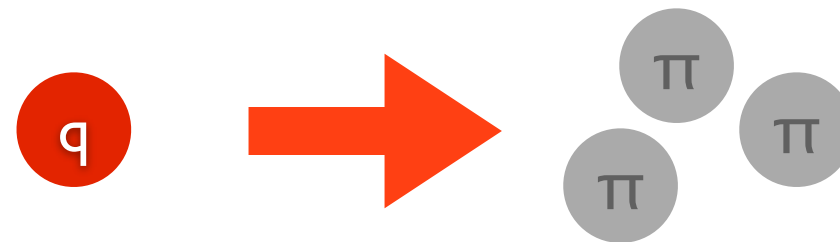


# Parton $\rightarrow$ Hadrons?

## Early models: “Independent Fragmentation”

Local Parton Hadron Duality (LPHD) can give useful results for **inclusive** quantities in collinear fragmentation

Motivates a simple model:



## But ...

The point of confinement is that partons are coloured

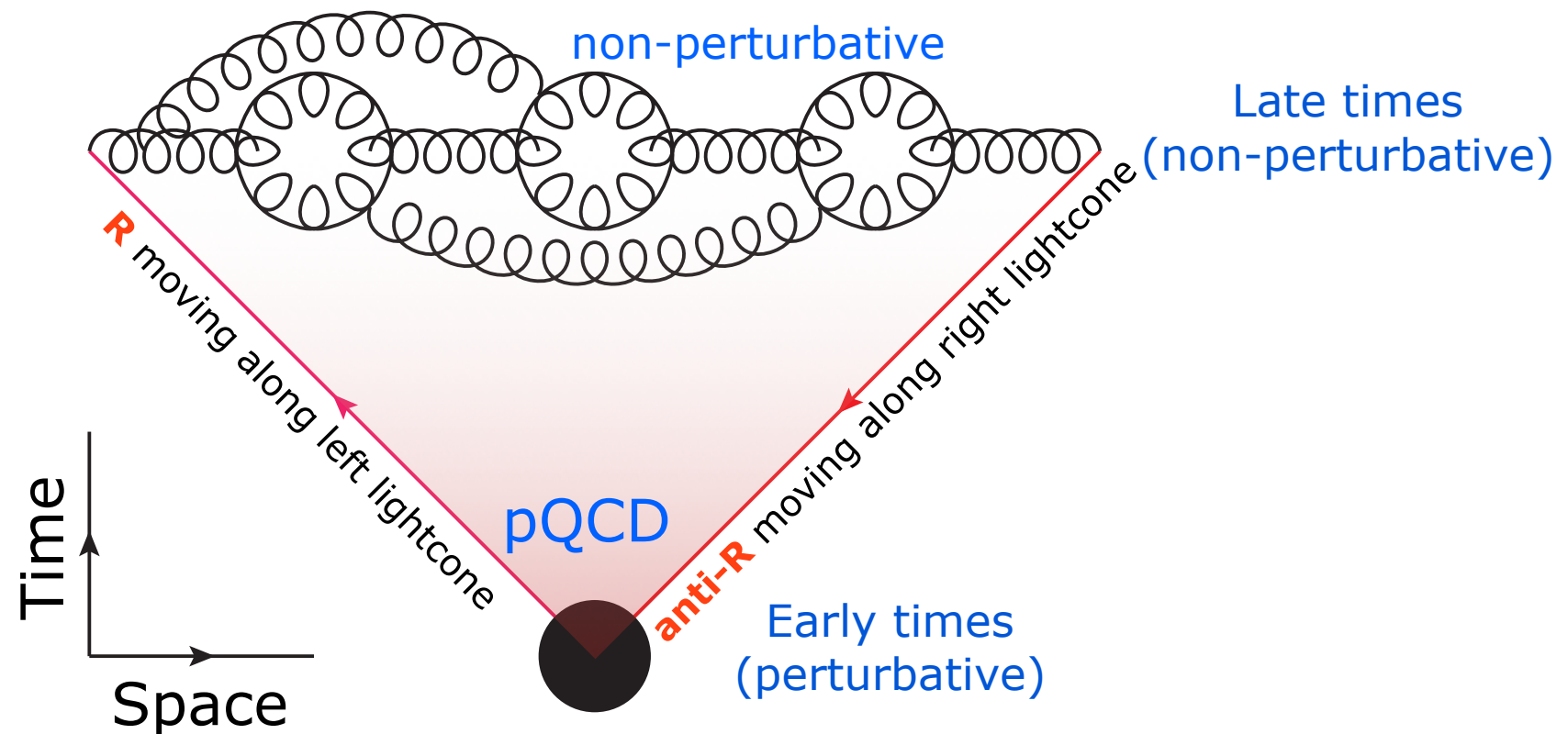
Hadronization = the process of colour neutralization

- $\rightarrow$  Unphysical to think about independent fragmentation of a single parton into hadrons
- $\rightarrow$  Too naive to see LPHD (inclusive) as a justification for Independent Fragmentation (exclusive)
- $\rightarrow$  More physics needed

# Colour Neutralization

## A physical hadronization model

Should involve at least **2** partons, with opposite color charges (e.g., **R** and **anti-R**)

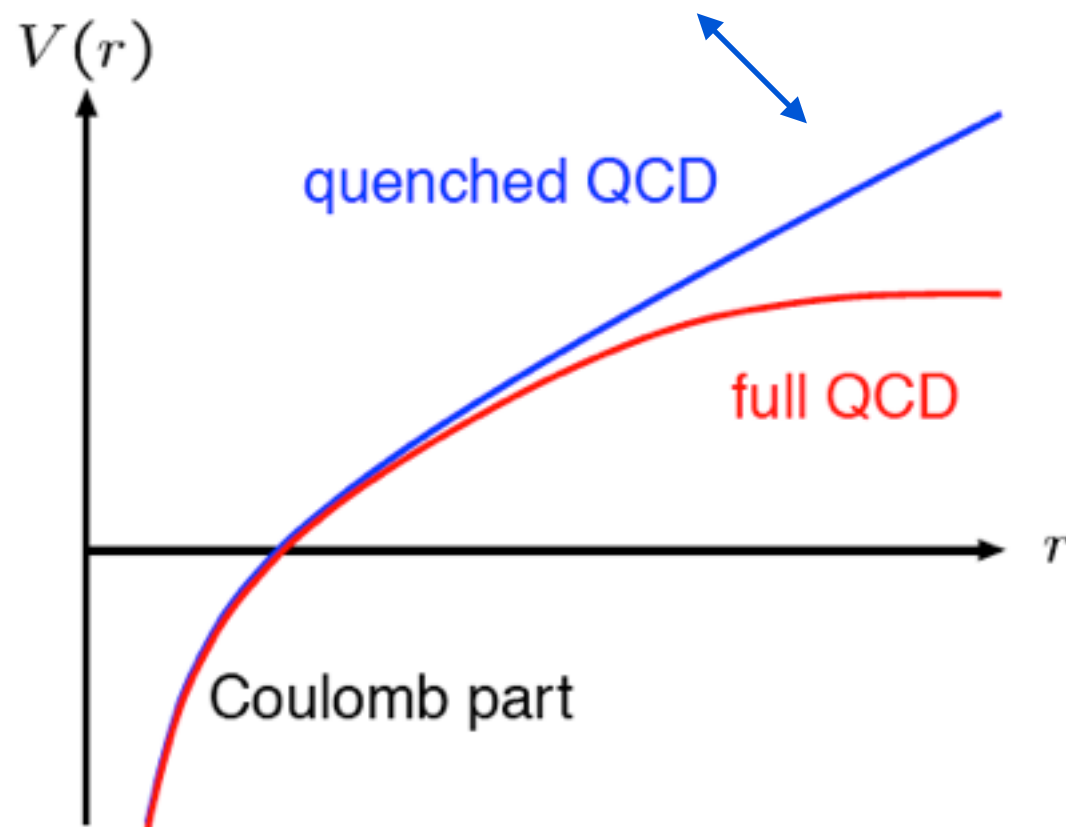


Strong “confining” field emerges between the two charges when their separation  $> \sim 1\text{fm}$

# Linear Confinement → Strings

## Lattice QCD

Linear potential (without string breaks)



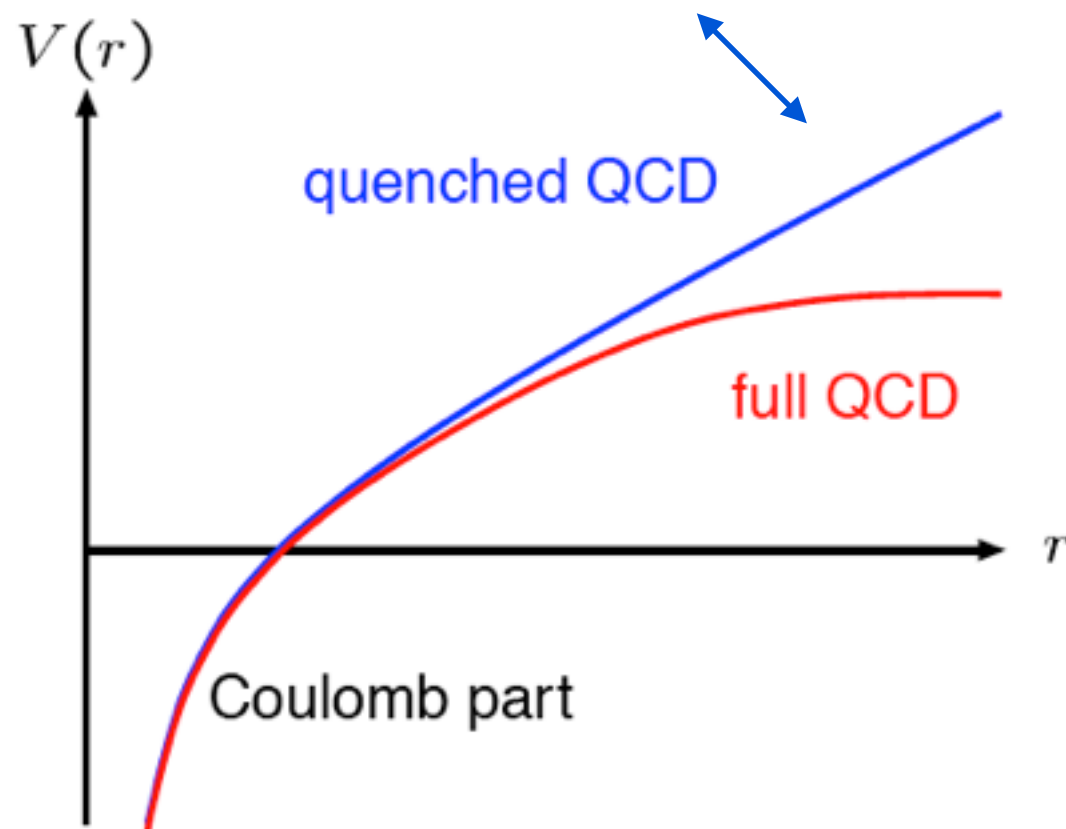
Illustrations by  
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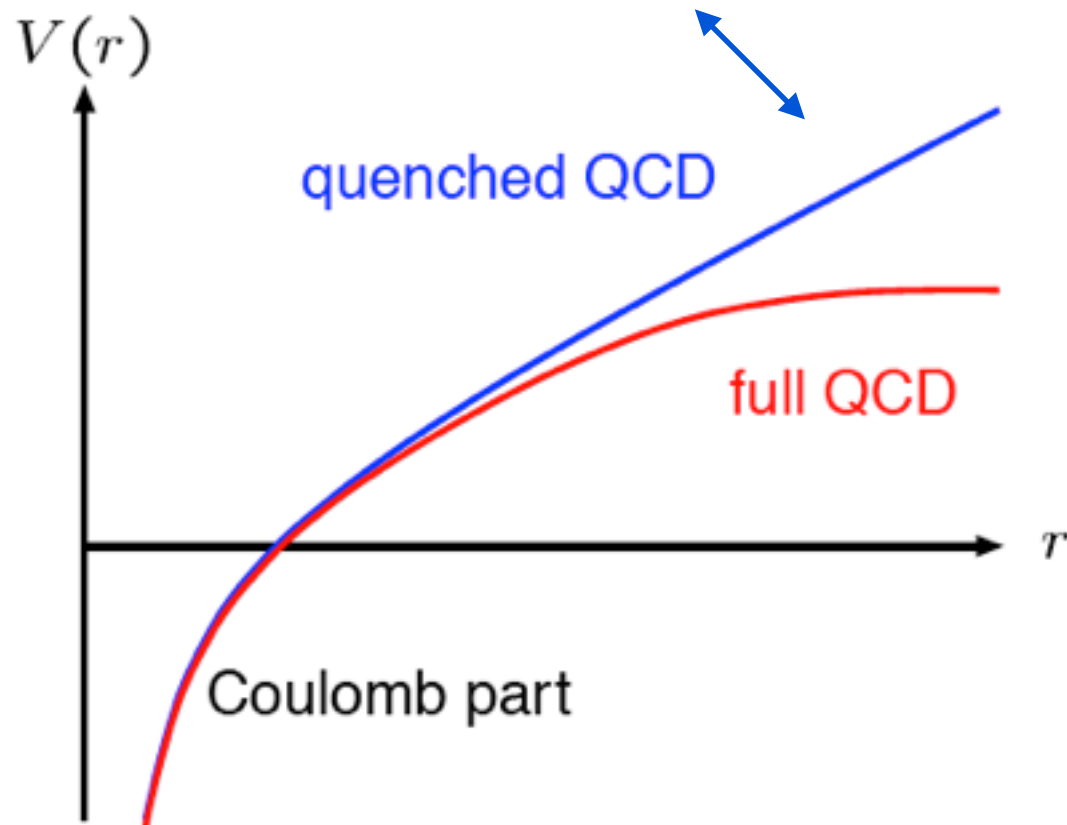
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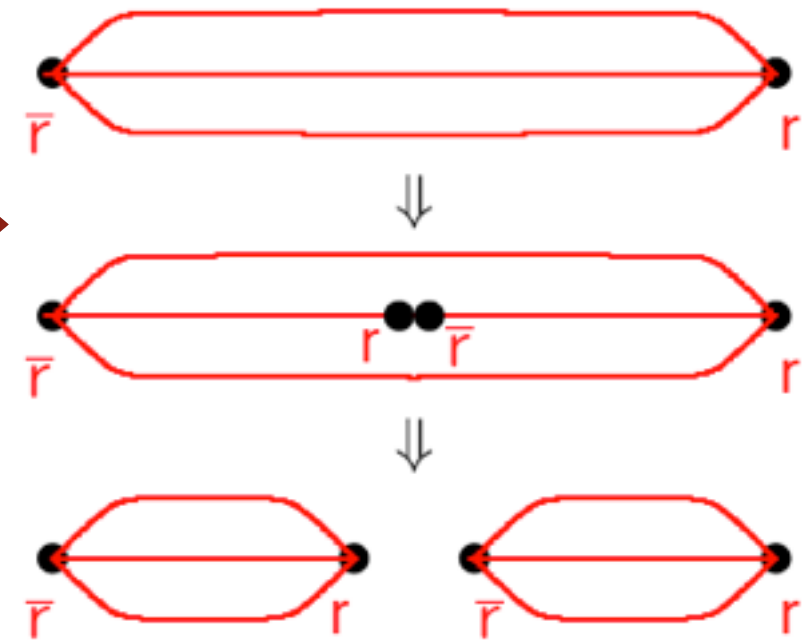


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## Lund Model

+ string breaks via Quantum Tunneling



(simplified colour representation)

$$\mathcal{P} \propto \exp\left(\frac{-m_q^2 - p_{\perp}^2}{\kappa/\pi}\right)$$

- Gaussian  $p_T$  spectrum (string tension = tuning parameter)
- Heavier quarks suppressed.  $\text{Prob}(q=d,u,s,c) \approx 1 : 1 : 0.2 : 10^{-11}$

Illustrations by  
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# Iterative String Breaks

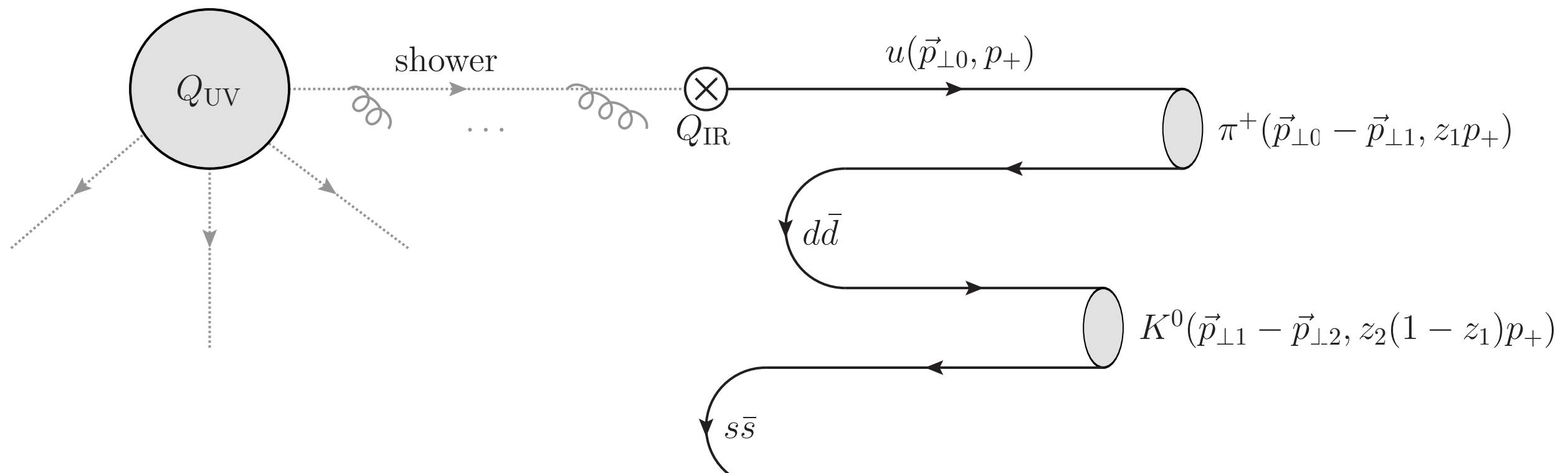
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**Iterate** String  $\rightarrow$  Hadron + String'

**Causality** + Left-Right Symmetry:

$$f(z) \propto \frac{1}{z} (1-z)^a \exp\left(-\frac{b(m_h^2 + p_{\perp h}^2)}{z}\right)$$

Lund Symmetric String Fragmentation Function



The Lund





# Tuning

means different things to different people





# Tuning

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10% agreement is great  
for (N)LO + LL

MB/UE/Soft: larger  
uncertainties since driven  
by non-factorizable and  
non-perturbative physics

Complicated dynamics:  
"If a model is simple, it is  
wrong" (*T. Sjöstrand*)







# Recent PYTHIA Models/Tunes

**Note:** I focus on default / author tunes here  
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## Aims for the Monash 2013 Tune

Monash 2013 Tune: e-Print: [arXiv:1404.5630](https://arxiv.org/abs/1404.5630)

Set M13 Tune:  
→  
in PYTHIA 8

Tune:ee = 7  
Tune:pp = 14

- Revise (and document) constraints from  $e^+e^-$  measurements
  - In particular in light of possible interplays with LHC measurements
- Test drive the new NNPDF 2.3 LO PDF set (with  $\alpha_s(m_Z) = 0.13$ ) for pp & ppbar
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## PYTHIA 6.4 (*warning: no longer actively developed*)

Default: still rather old  $Q^2$ -ordered tune ~ Tevatron Tune A

Most recent: Perugia 2012 set of  $p_T$ -ordered tunes (370 - 382) + Innsbruck (IBK) Tunes (G. Rudolph)

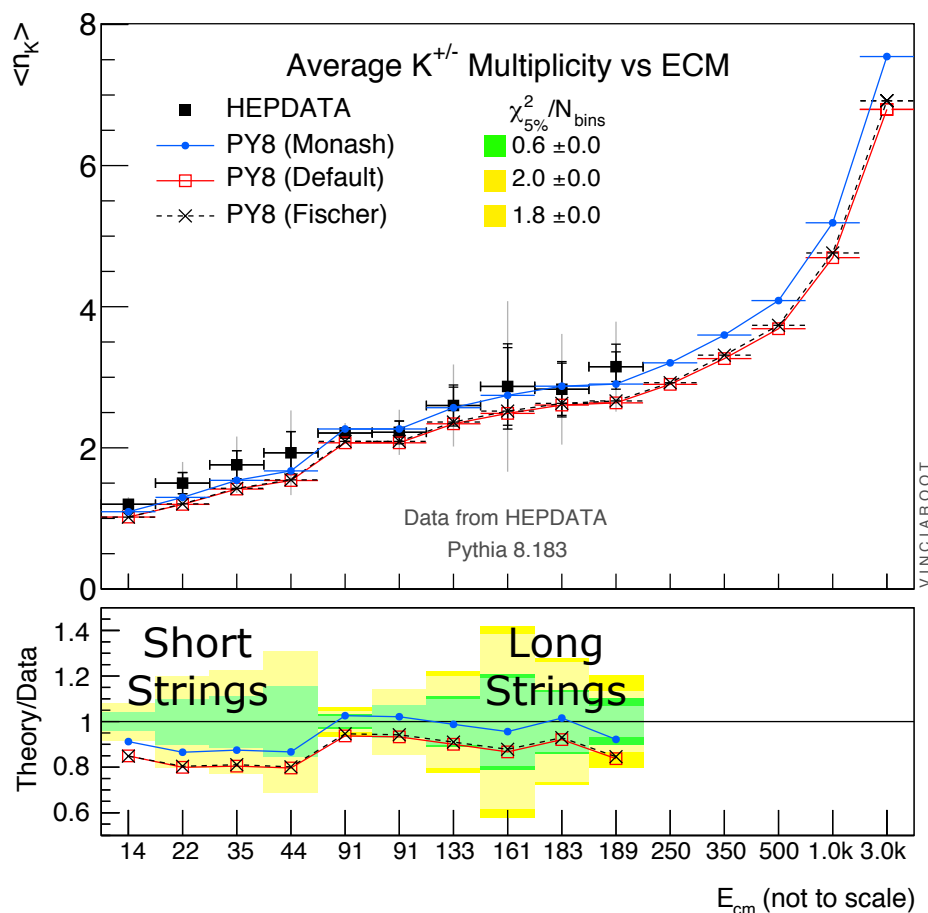
Perugia Tunes: e-Print: [arXiv:1005.3457](https://arxiv.org/abs/1005.3457)  
(+ 2011 & 2012 updates added as appendices)



# Monash 2013 Tune Highlights

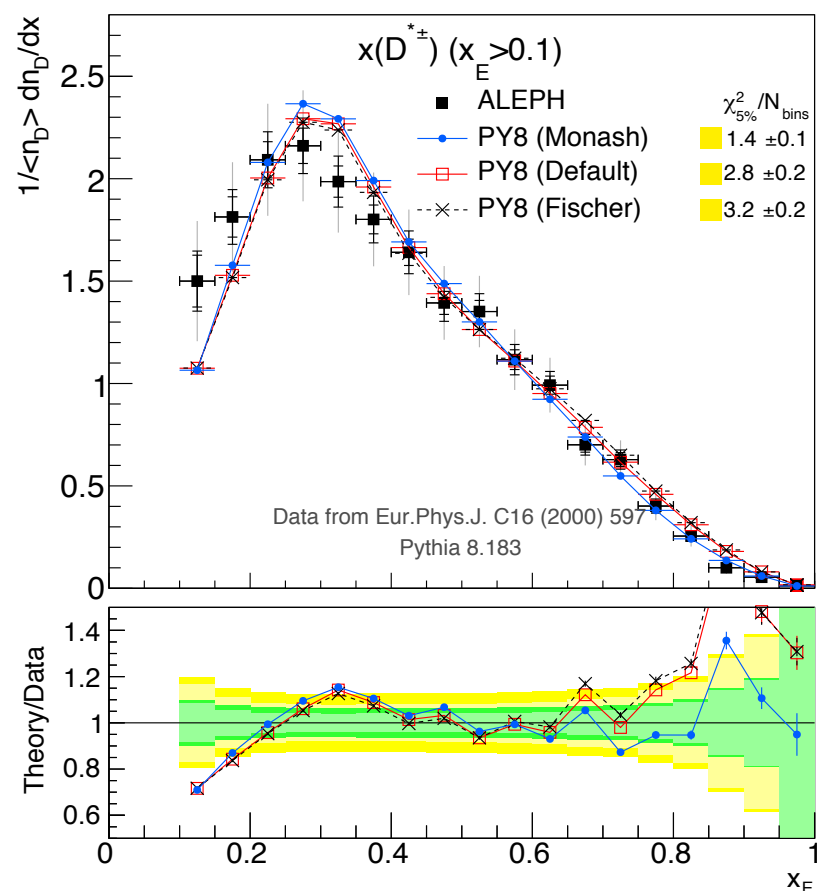
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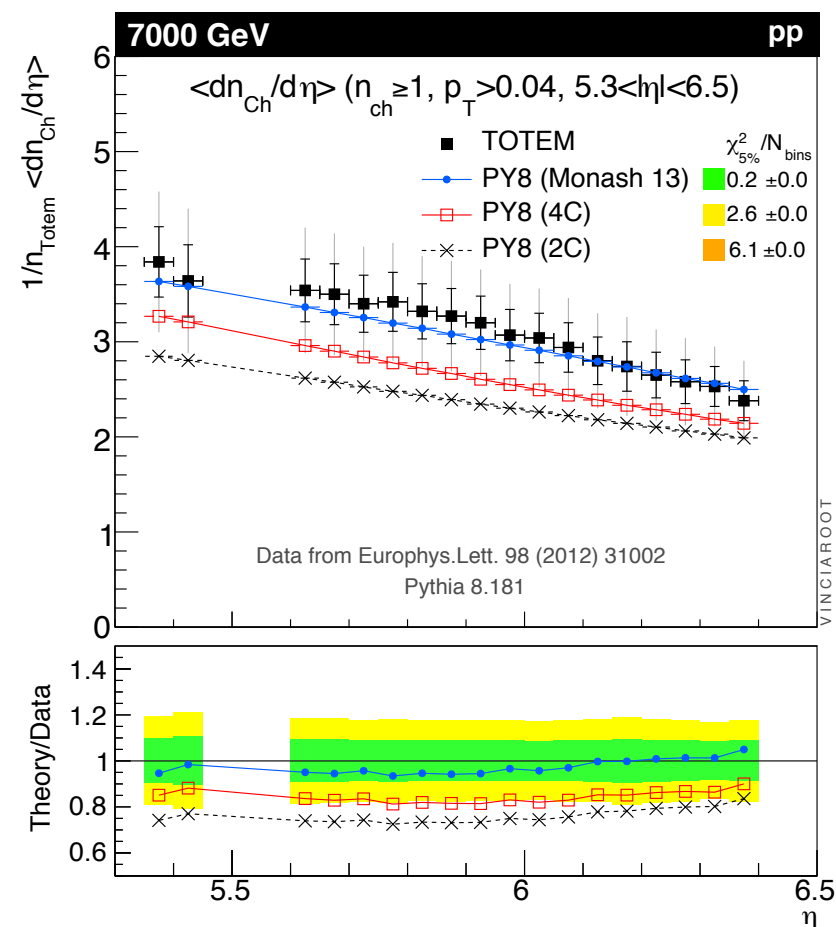
Better agreement with ee identified-strange measurements across all energies, and with Kaons at LHC

Softer D and B spectra near  $z = 1$



Ultra-hard tail of c and b fragmentation agrees better with LEP and SLD, including event shapes in b-tagged events

More forward activity



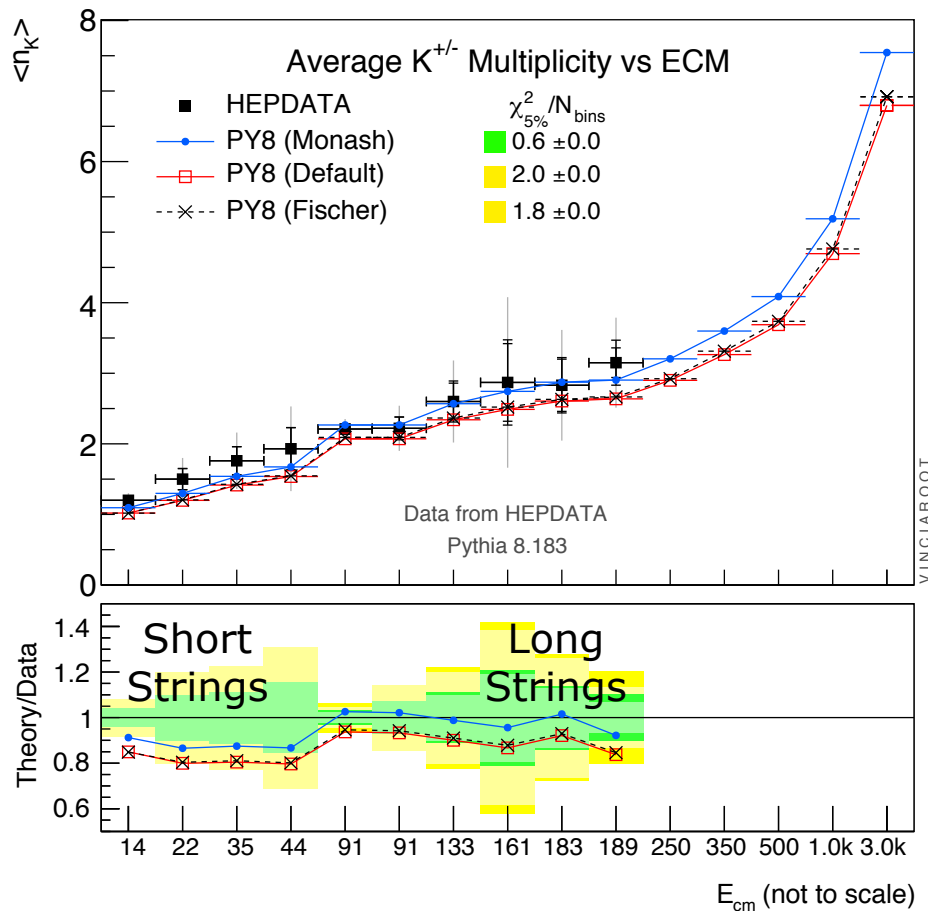
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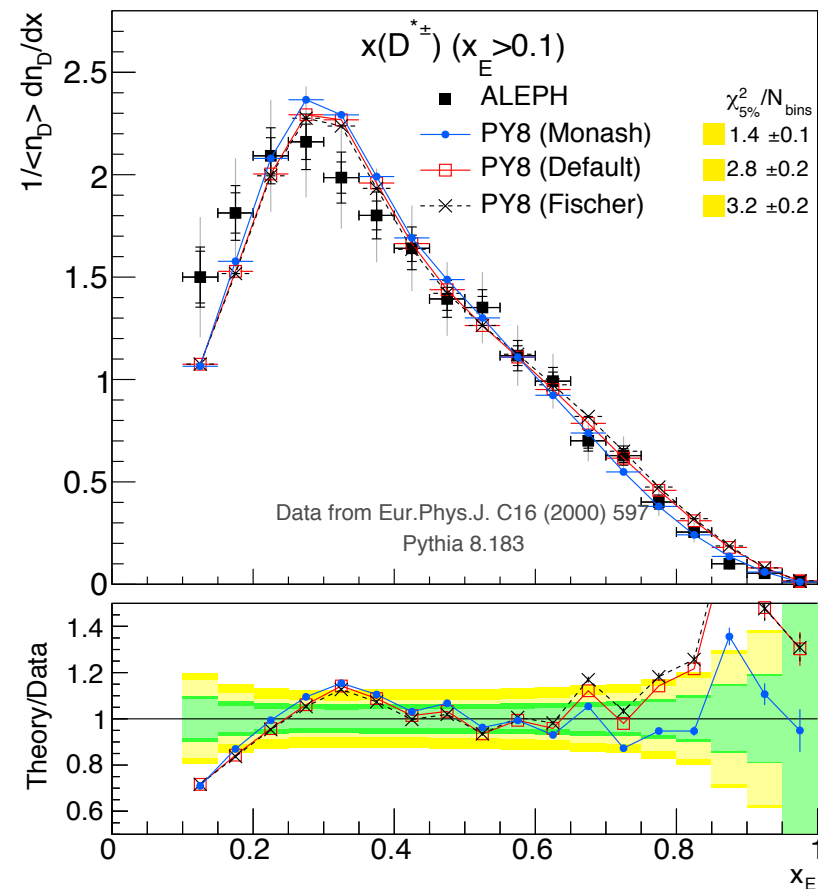
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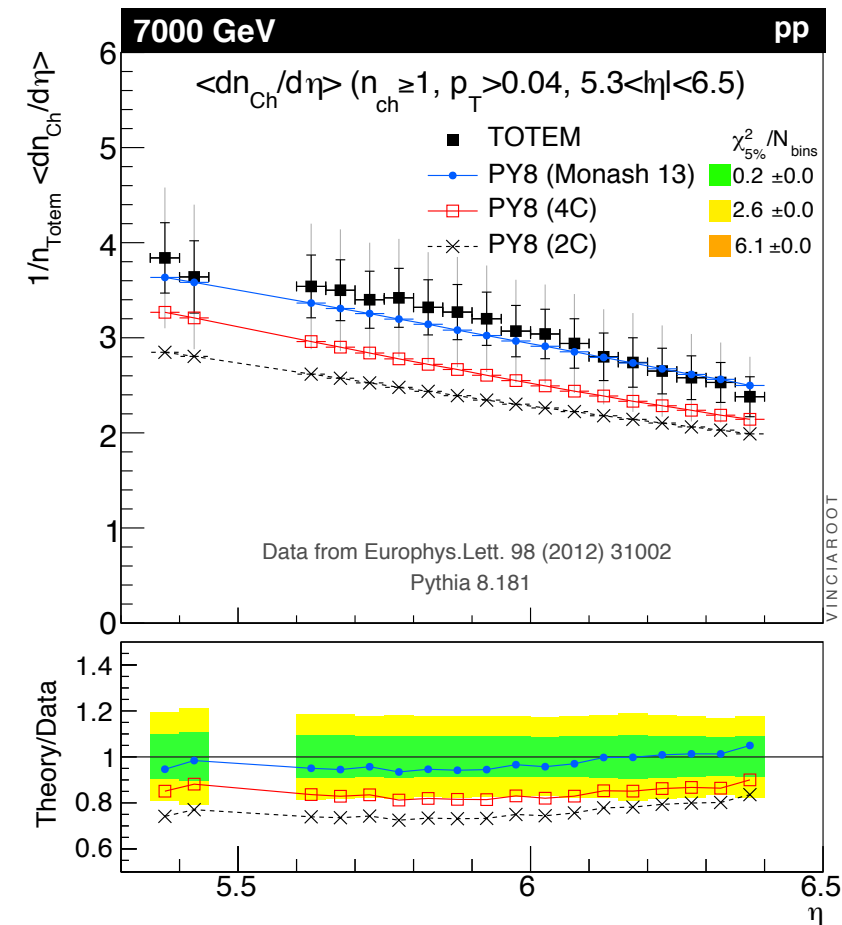
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Monash  
Warwick  
Alliance

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The role and modeling of diffraction from low to high masses (including UE in diffractive jet events?)  $\leftrightarrow$  Hard Diffraction, Factorization, CR

**New:**  
Monash  
Warwick  
Alliance



# Puzzles (a selection of)

Identified-particle  $p_T$  spectra at LHC

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Gluon/Quark discrimination and  $G \rightarrow QQ$  splittings in gluon jets

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# Summary

## QCD phenomenology is witnessing a rapid evolution:

Driven by demand of **high precision** for LHC environment

**Exploring physics:** infinite-order structure of quantum field theory. Universalities vs process-dependence.

Emergent QCD phenomena: **Jets, Strings, Hadrons**

## Non-perturbative QCD is still hard

Lund string model remains best bet, but  $\sim 30$  years old

Lots of input from LHC to spur model building. **Aims for run 2?**

## “Solving the LHC” is both interesting and rewarding

New ideas evolving on both perturbative and non-perturbative sides  $\rightarrow$  many opportunities for theory-experiment interplay

**Key to high precision**  $\rightarrow$  max information about the Terascale



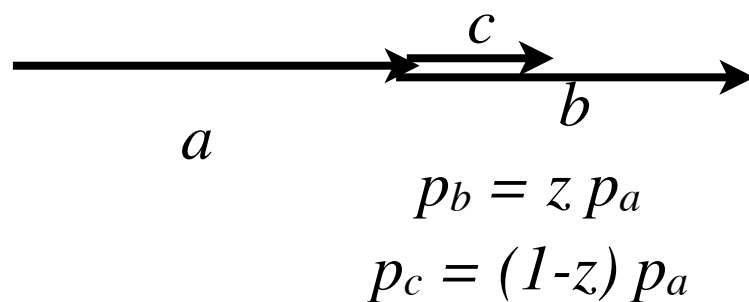
# What's the evolution kernel?

## DGLAP splitting functions

Can be derived from *collinear limit* of MEs  $(p_b + p_c)^2 \rightarrow 0$   
 + evolution equation from invariance with respect to  $Q_F \rightarrow RGE$

DGLAP  
 (E.g., PYTHIA)

$$d\mathcal{P}_a = \sum_{b,c} \frac{\alpha_{abc}}{2\pi} P_{a \rightarrow bc}(z) dt dz .$$



$$P_{q \rightarrow qg}(z) = C_F \frac{1+z^2}{1-z} ,$$

$$P_{g \rightarrow gg}(z) = N_C \frac{(1-z(1-z))^2}{z(1-z)} ,$$

$$P_{g \rightarrow q\bar{q}}(z) = T_R (z^2 + (1-z)^2) ,$$

$$P_{q \rightarrow q\gamma}(z) = e_q^2 \frac{1+z^2}{1-z} ,$$

$$P_{l \rightarrow l\gamma}(z) = e_l^2 \frac{1+z^2}{1-z} ,$$

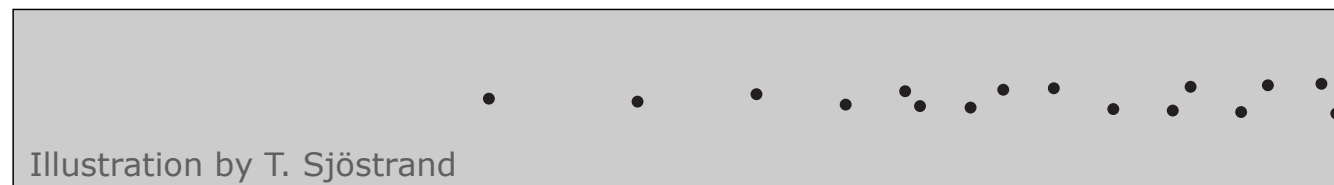
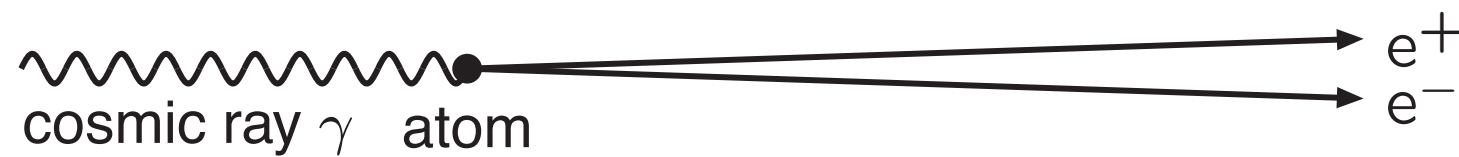
$$dt = \frac{dQ^2}{Q^2} = d \ln Q^2$$

... with  $Q^2$  some measure of "hardness"  
 = event/jet resolution  
 measuring parton virtualities / formation time / ...

**Note:** there exist now also alternatives to AP kernels (with same collinear limits!): dipoles, antennae, ...

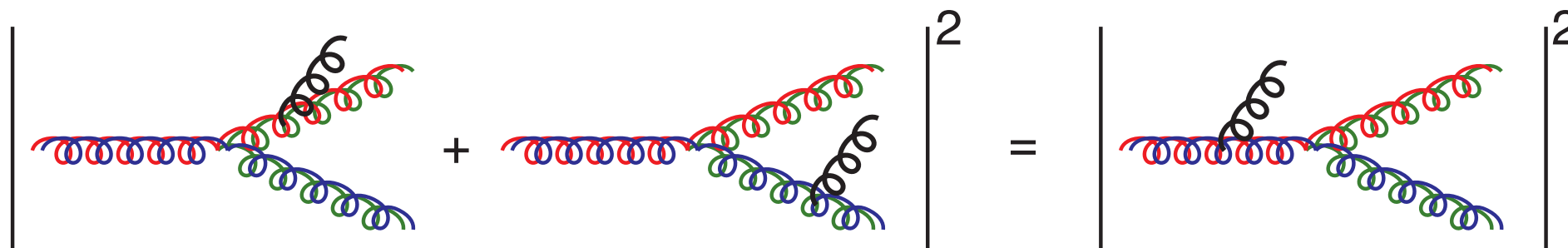
# Coherence

## QED: Chudakov effect (mid-fifties)



emulsion plate      reduced ionization      normal ionization

## QCD: colour coherence for **soft** gluon emission



→ an example of an interference effect that can be treated probabilistically

More interference effects can be included by matching to full matrix elements

# Coherence

## QED: Chudakov effect (mid-fifties)

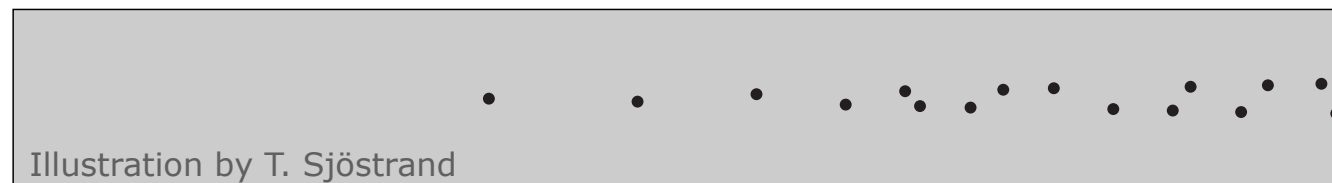
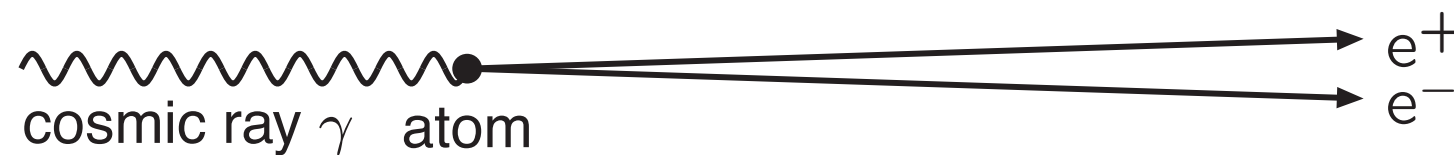


Illustration by T. Sjöstrand

emulsion plate

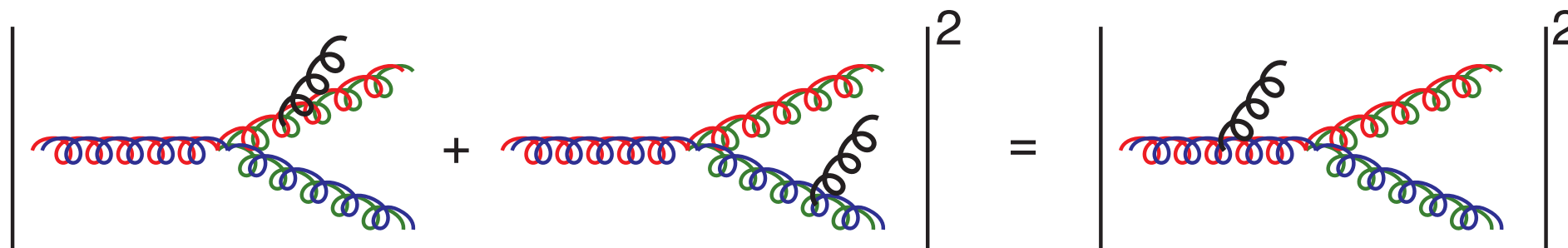
reduced  
ionization

normal  
ionization

Approximations to  
Coherence:

- Angular Ordering (HERWIG)
- Angular Vetos (PYTHIA)
- Coherent Dipoles/Antennae (ARIADNE, Catani-Seymour, VINCIA)

## QCD: colour coherence for **soft** gluon emission



→ an example of an interference effect that can be treated probabilistically

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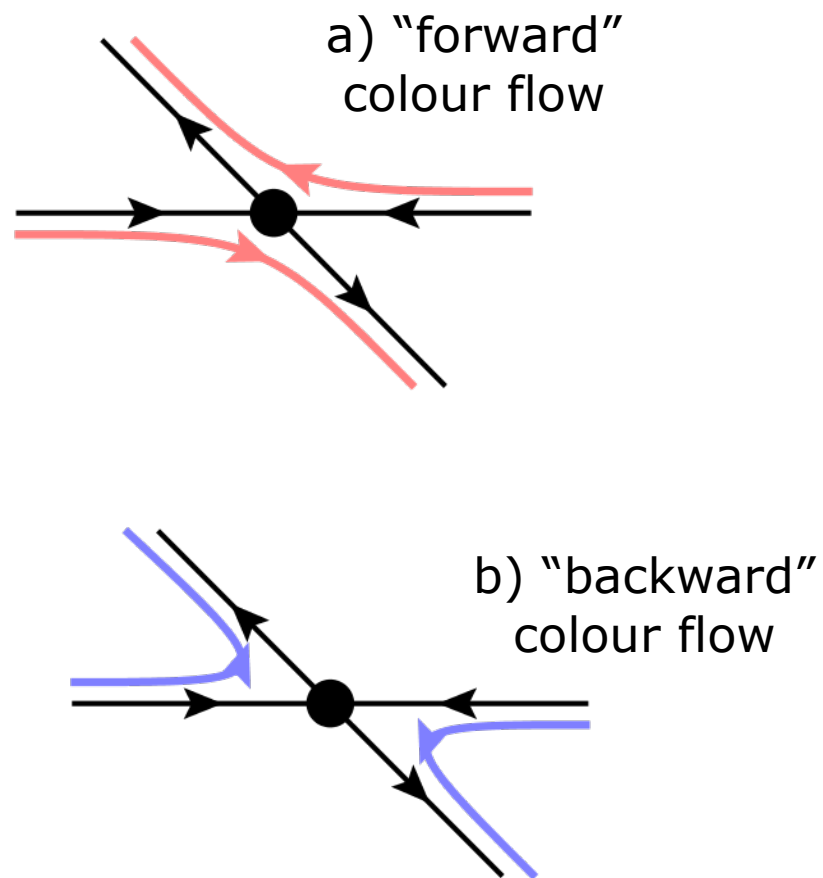


# Coherence at Work

Example taken from: Ritzmann, Kosower, PS, [PLB718 \(2013\) 1345](#)

## Example: quark-quark scattering in hadron collisions

Consider one specific phase-space point (eg scattering at  $45^\circ$ )  
2 possible colour flows: a and b



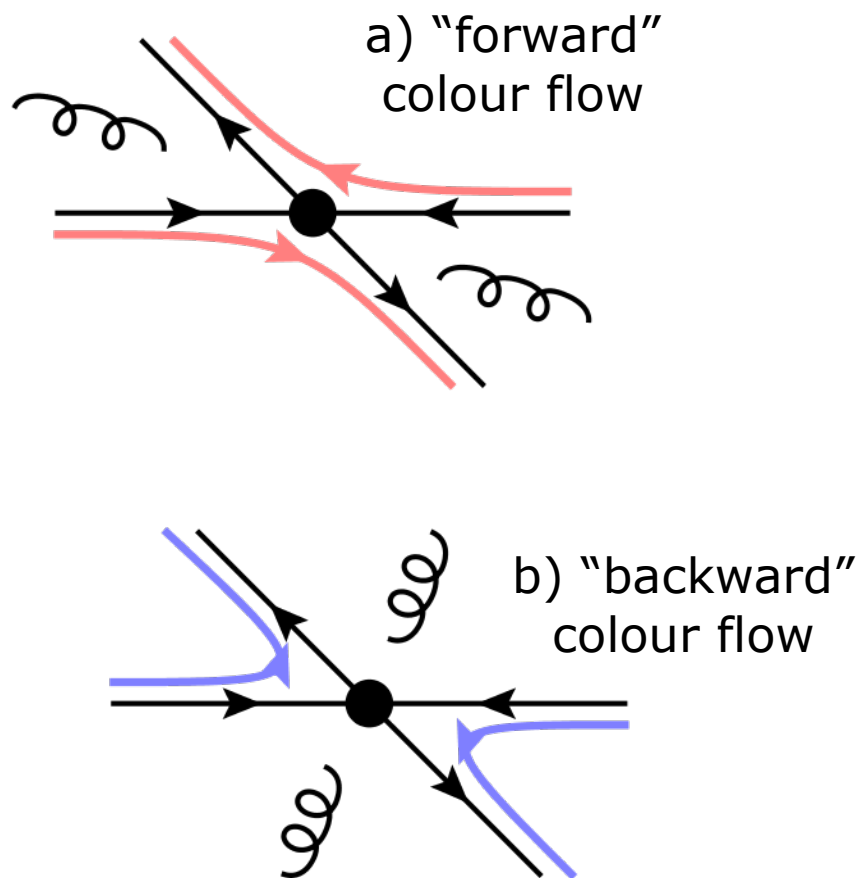
Another good recent example is the SM contribution to the Tevatron top-quark forward-backward asymmetry from coherent showers, see: PS, Webber, Winter, JHEP 1207 (2012) 151

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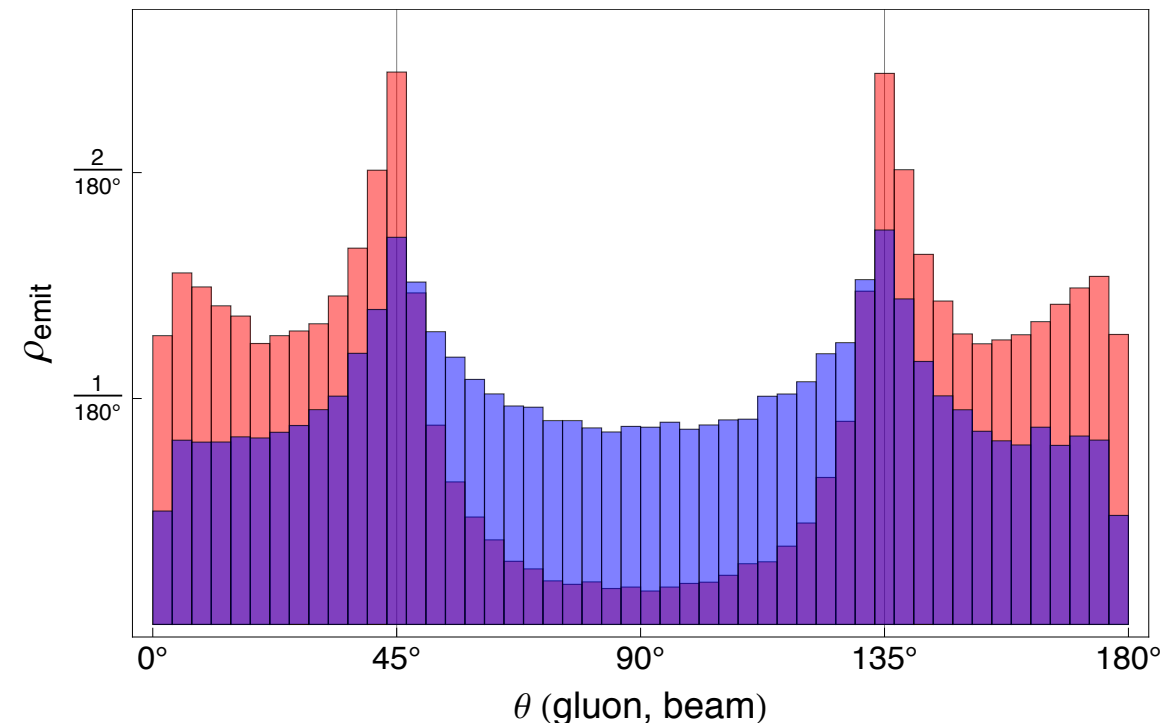
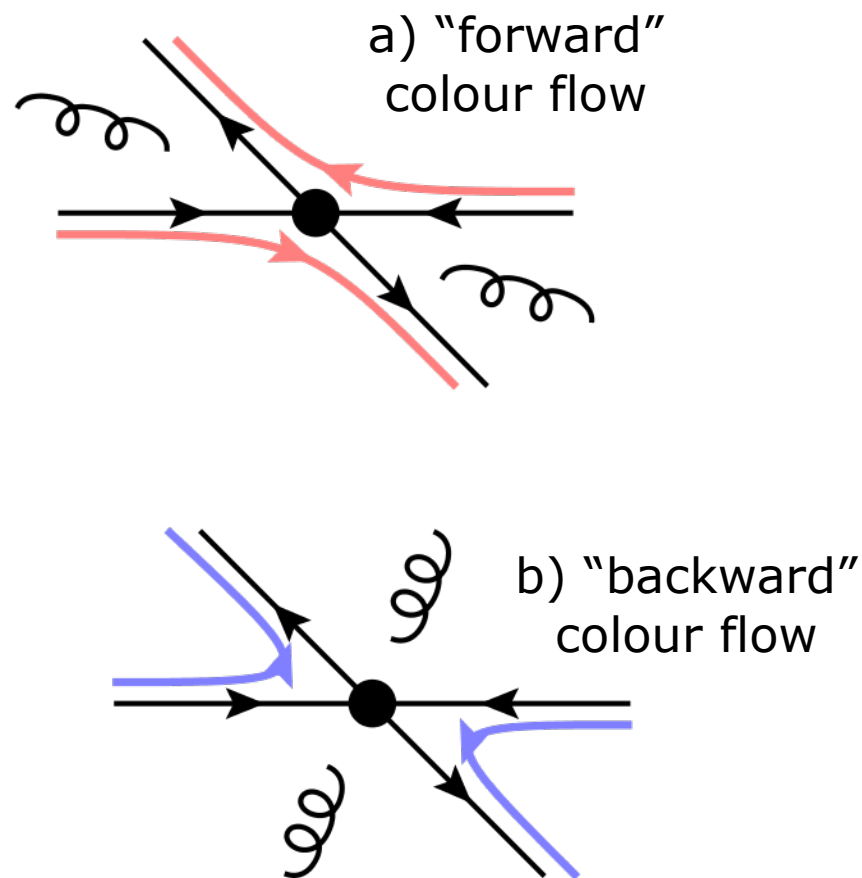


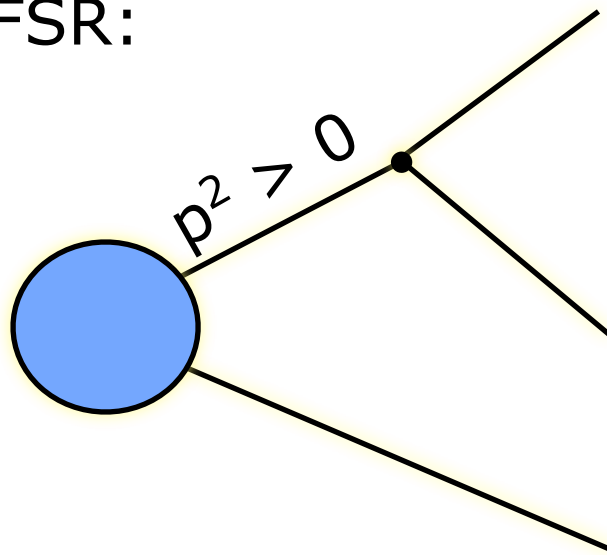
Figure 4: Angular distribution of the first gluon emission in  $qq \rightarrow qq$  scattering at  $45^\circ$ , for the two different color flows. The light (red) histogram shows the emission density for the forward flow, and the dark (blue) histogram shows the emission density for the backward flow.

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# Initial-State vs Final-State Evolution

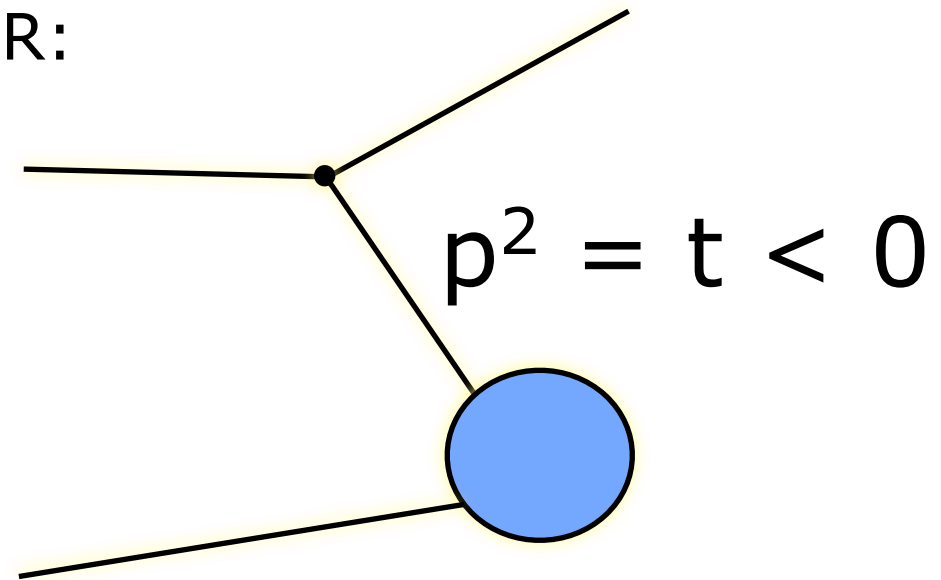
FSR:



Virtualities are  
Timelike:  $p^2 > 0$

Start at  $Q^2 = Q_F^2$   
"Forwards evolution"

ISR:



Virtualities are  
Spacelike:  $p^2 < 0$

Start at  $Q^2 = Q_F^2$   
Constrained backwards evolution  
towards boundary condition = proton

Separation meaningful for collinear radiation, but not for soft ...